

# Present/Future Neutron Optics

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# Phase Space Density (Brilliance)

ESS, SNS-STS, J-PARC TS-2

# J-PARC MLF 2nd Target Station

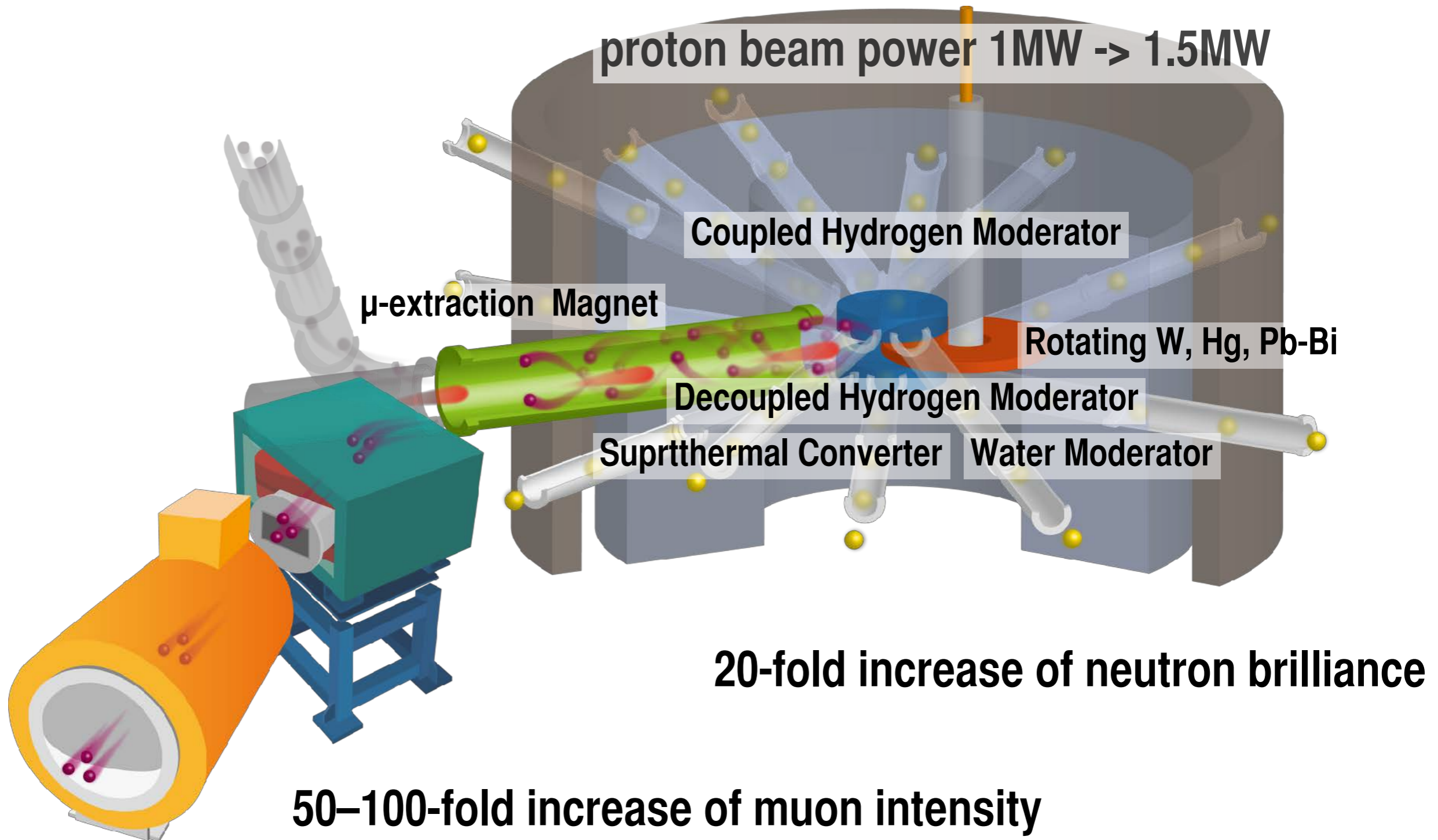
## Conceptual Design ver.1.1 (2019/03/22)





# J-PARC MLF 2nd Target Station

Conceptual Design ver.1.1 (2019/03/22)



# muon science

Material and Life Science

Negative-muon  $\mu$ SR

Chemical Analysis with Muon-characteristic X-rays

Ultra-slow Muons

Surface Science

Micro-muon Beam for 2d- and 3d-scanning Imaging

Transmission Muon Microscopy

Soft- and Hard-error of Electronic Devices

Muon g-2/EDM

Hyperfine Structure of Muonium

Proton Radius

Muon-decay Parameters

Muon Rare Decays

Nuclear Study with Muons

# neutron science

## Material and Life Science

Elastic Scattering & Diffraction  
Hydrogen Collective Dynamics  
Vibrational and Magnetic Excitations  
Softmatters  
Holography for Active Sites  
Imaging

small-crystals (0.5mm -> 0.2mm)  
sample environment ( $T < 50\text{mK}$ ,  $P > 10\text{GPa}$ )  
transient phenomena (sub-msec)  
microscopic diffraction  
Protein Structural Analysis

## Neutron Transmission Microscope

Materials under High-pressures

Metallic Hydrogen      Planetary Science      Pressurized Ice

Materials under High Magnetic Fields

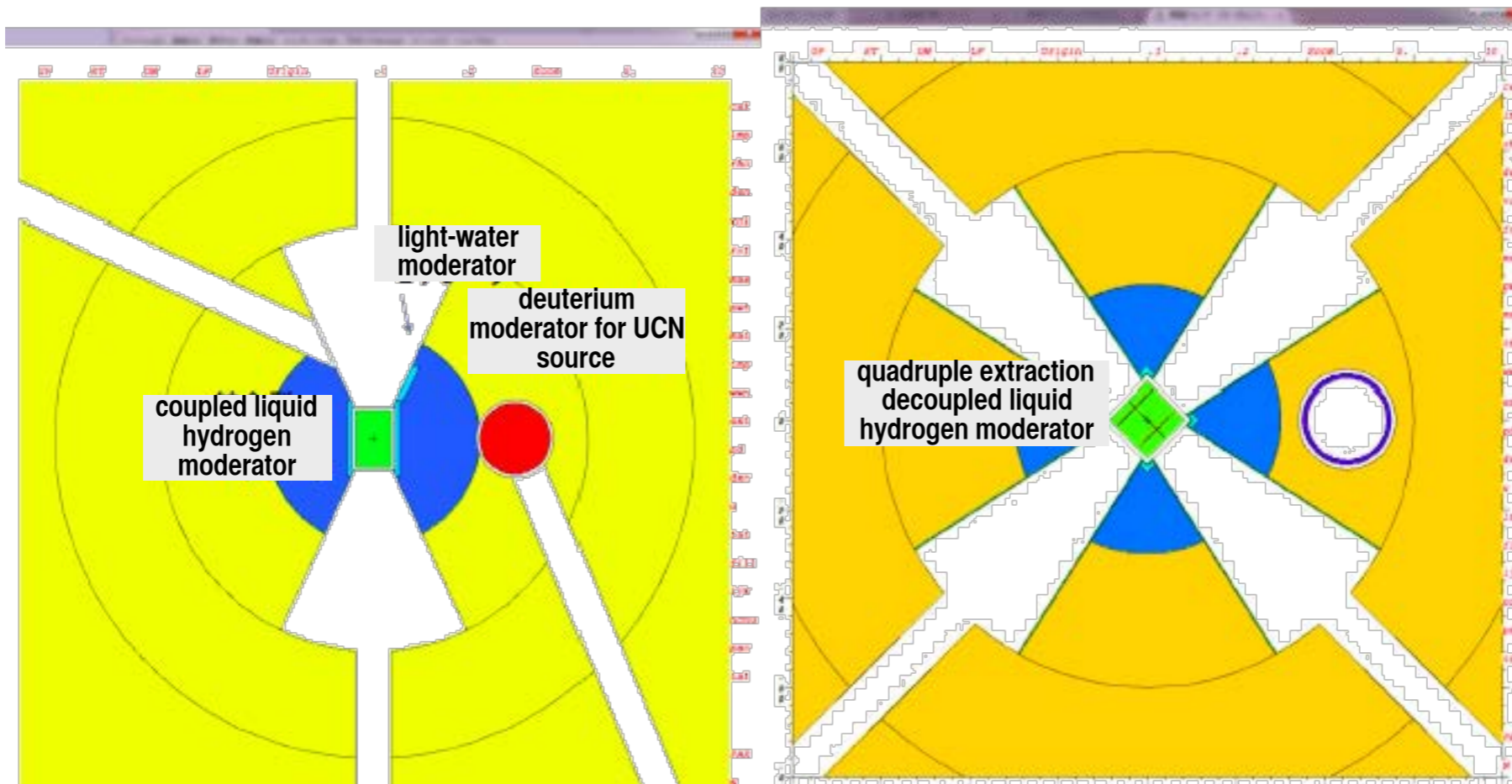
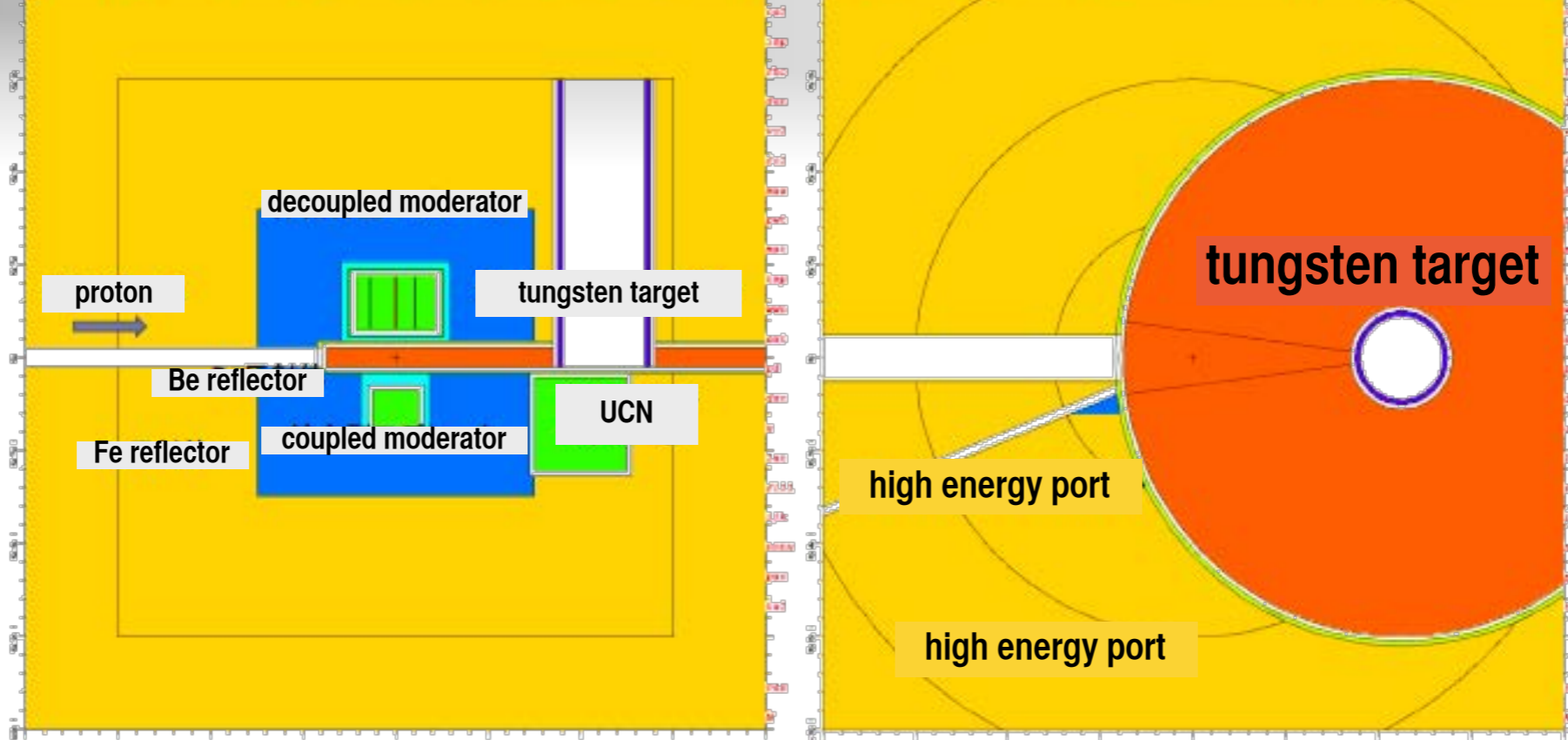
## Fundamental Physics

UCN      EDM      Gravitational Levels       $\beta$ -decay Parameters  
VCN      New Interaction Search      Scattering Lengths      Dark Energy Search  
VCN      Neutron-Antineutron Oscillation  
ETN (eV)      Discrete Symmetry Violations in Compound Nuclei -> TS1

## Nuclear Engineering

FN (MeV)      Nuclear Data      MeV Transmission Imaging

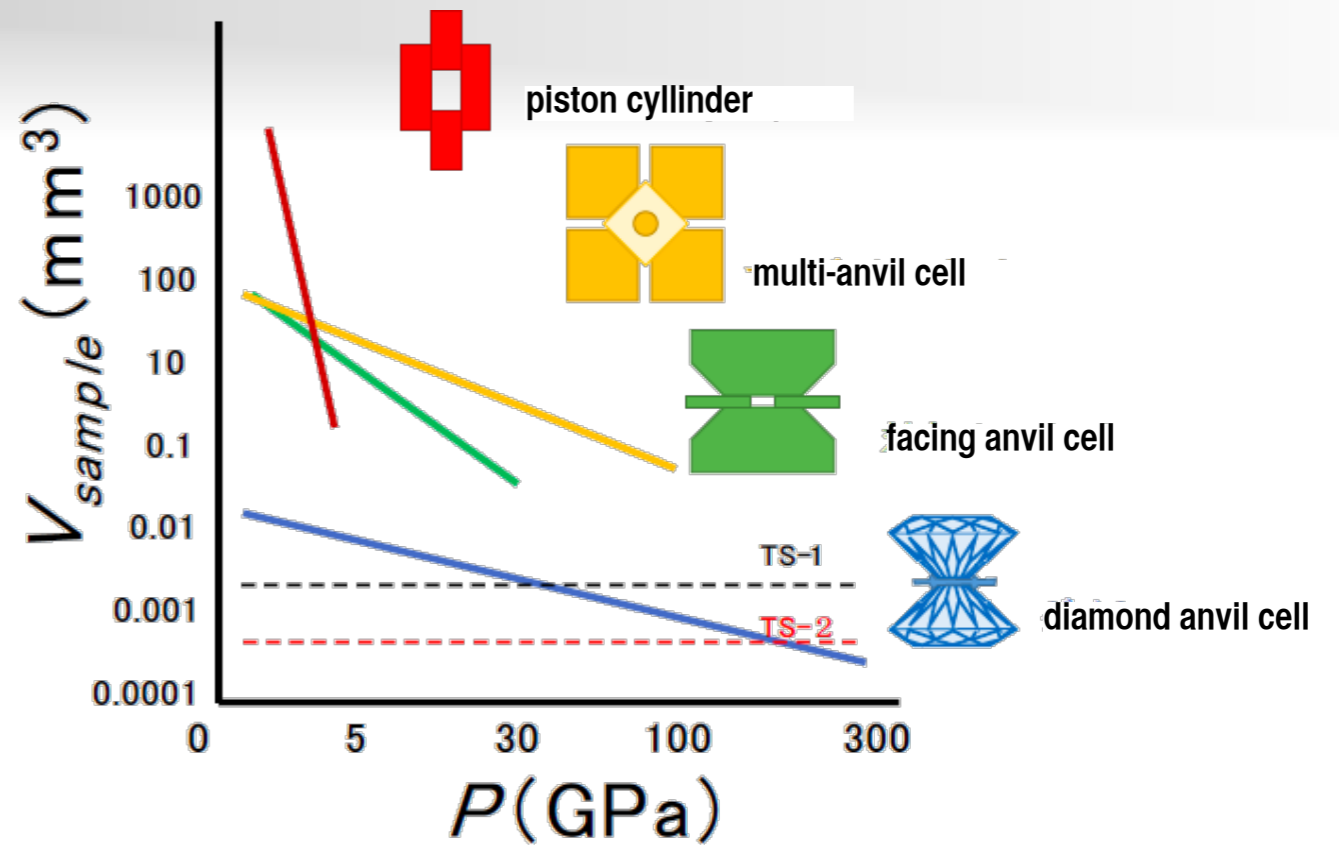




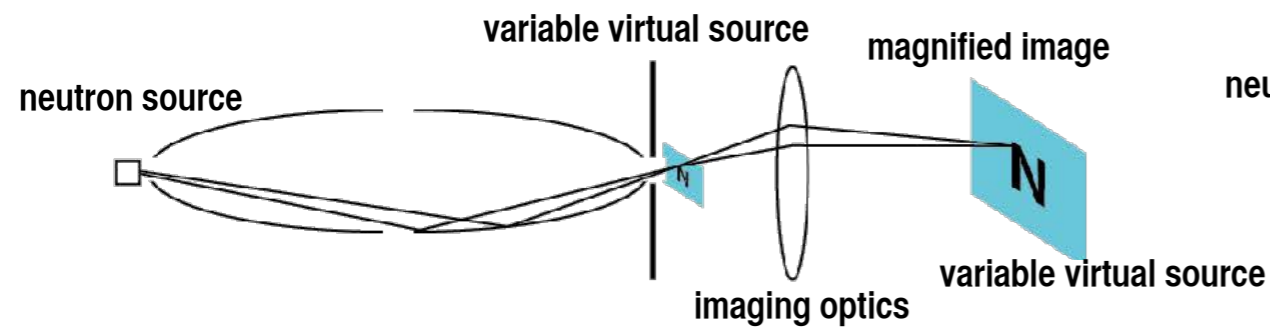
# brilliant neutron beam

## high phase-space-density

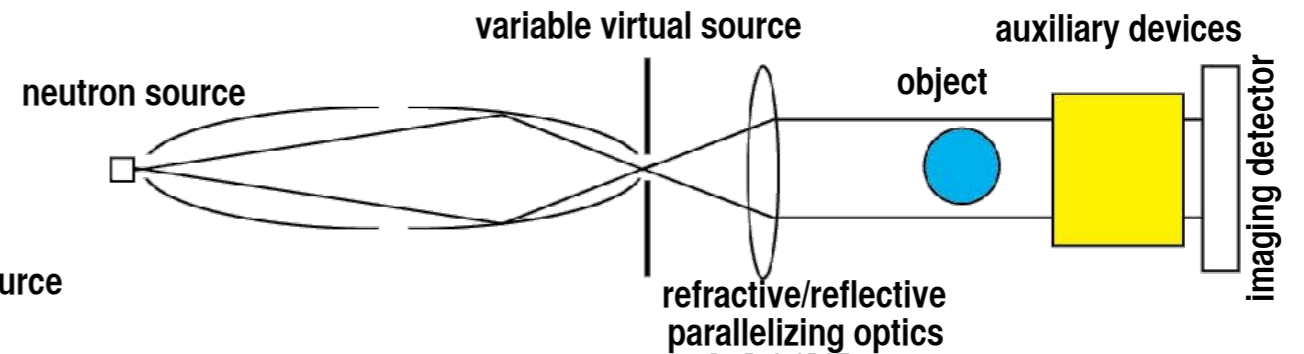
enables flexible optical control similar to photon optics



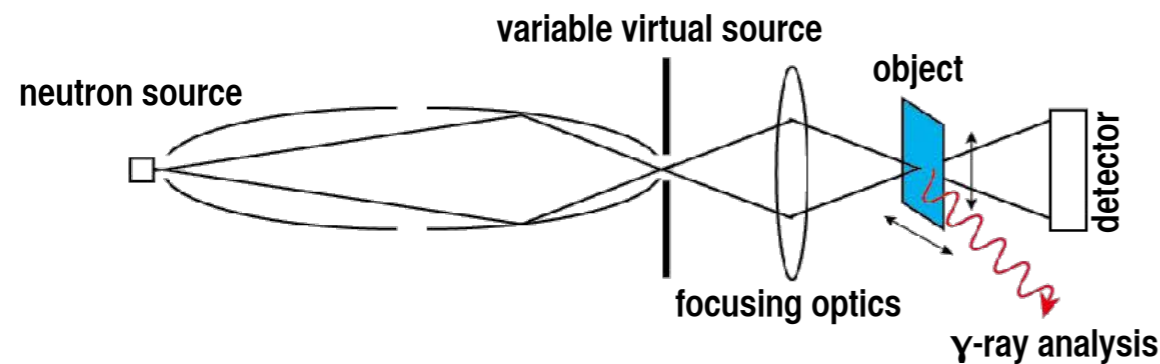
### high-resolution imaging



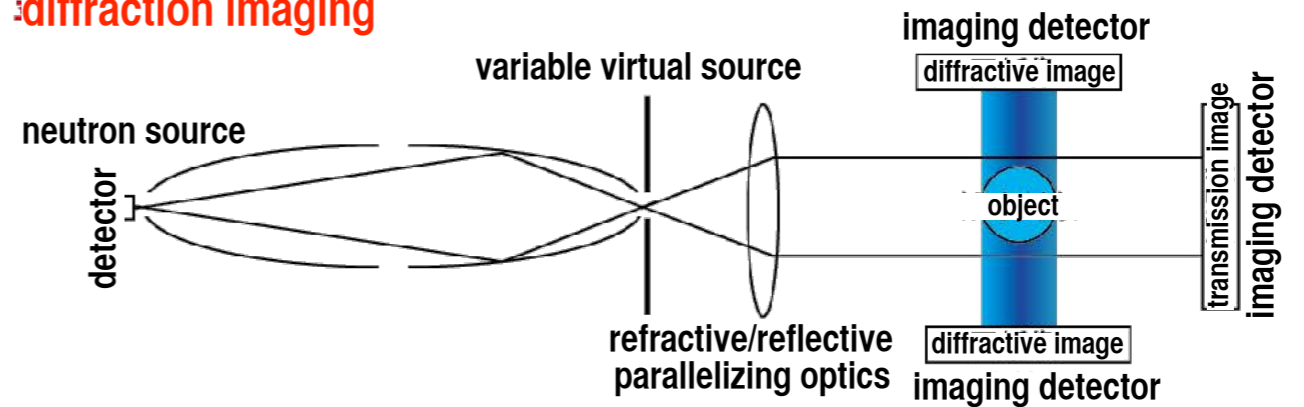
### versatile imaging



### scanning imaging, scanning prompt gamma-ray analysis

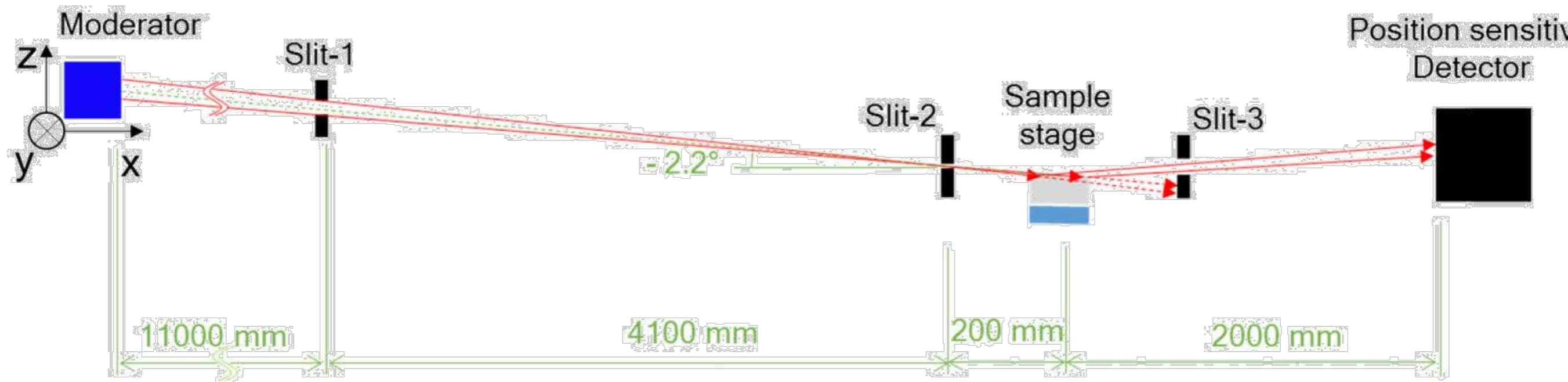


### diffraction imaging

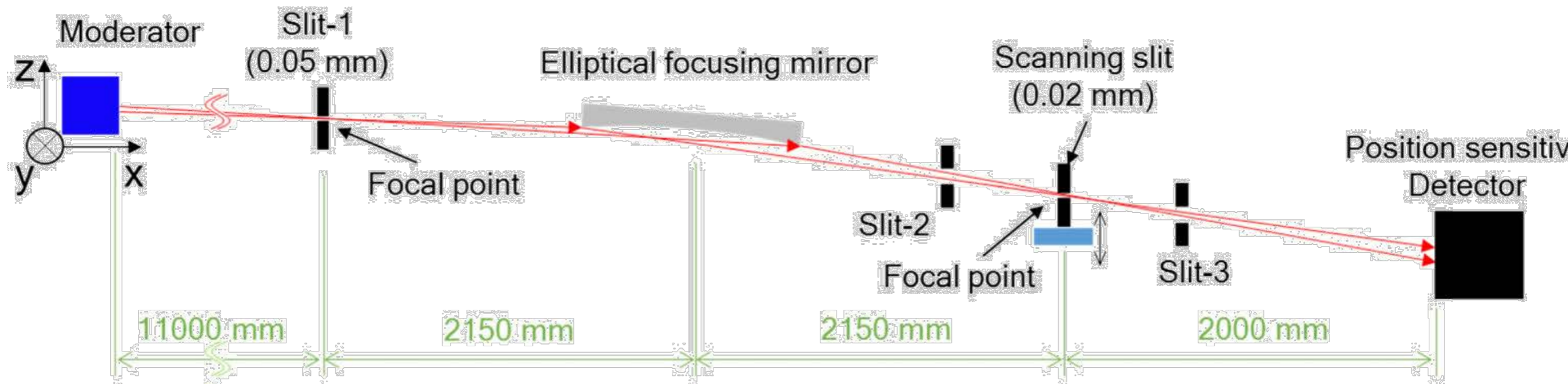




# focusing optics for reflectometry

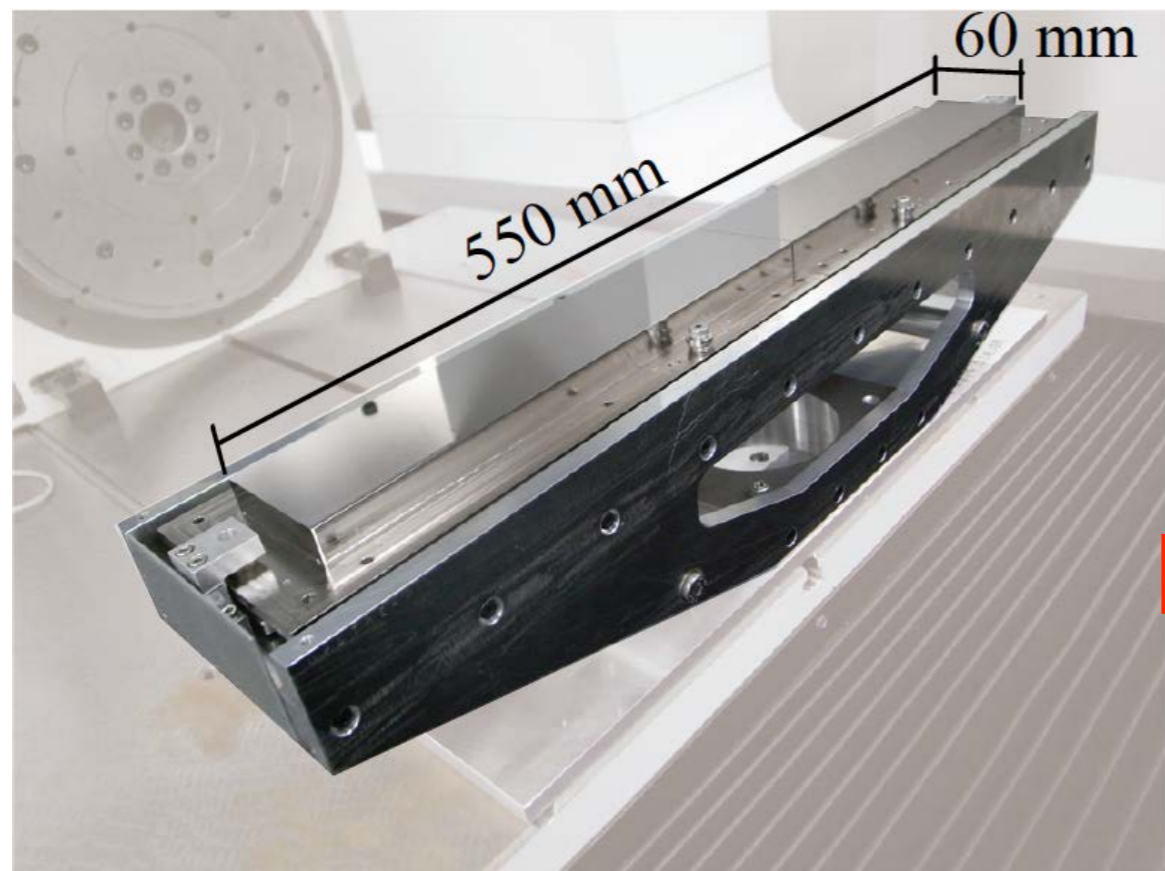


Schematic layout of SOFIA for the 2.2° inclined beamline.

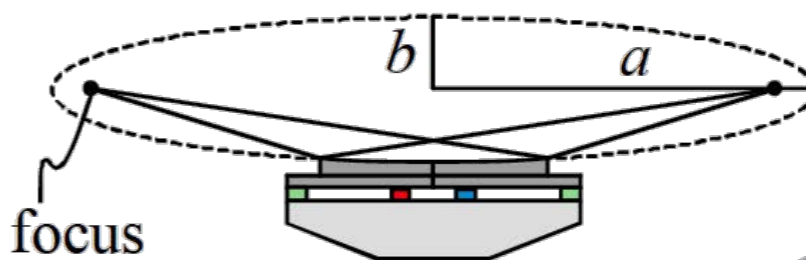


SOFIA with focusing optics

# focusing optics for reflectometry

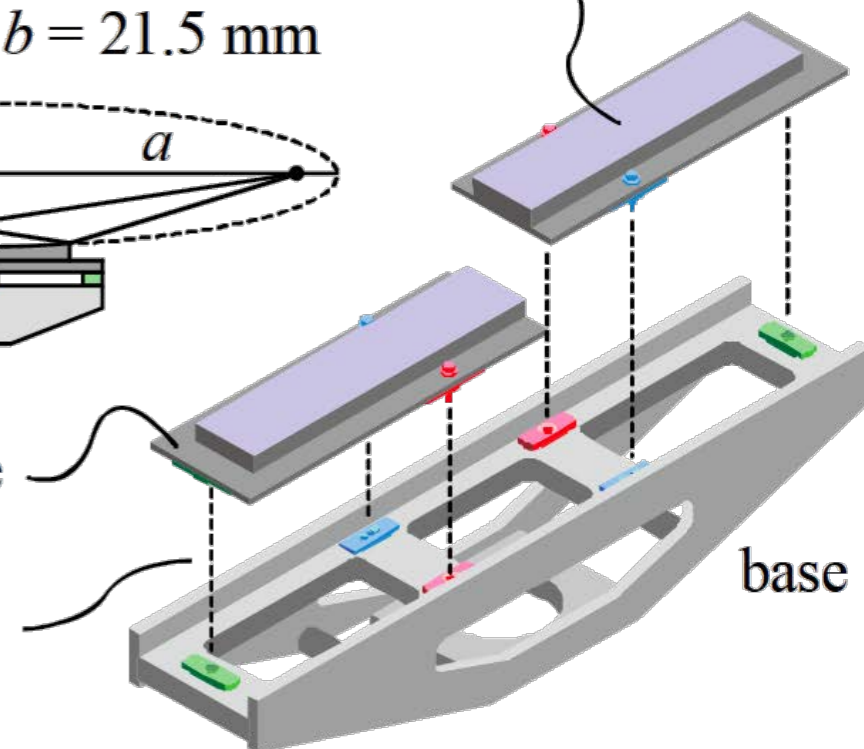


supermirror coating on elliptic surface  
 $a = 2150 \text{ mm}$ ,  $b = 21.5 \text{ mm}$



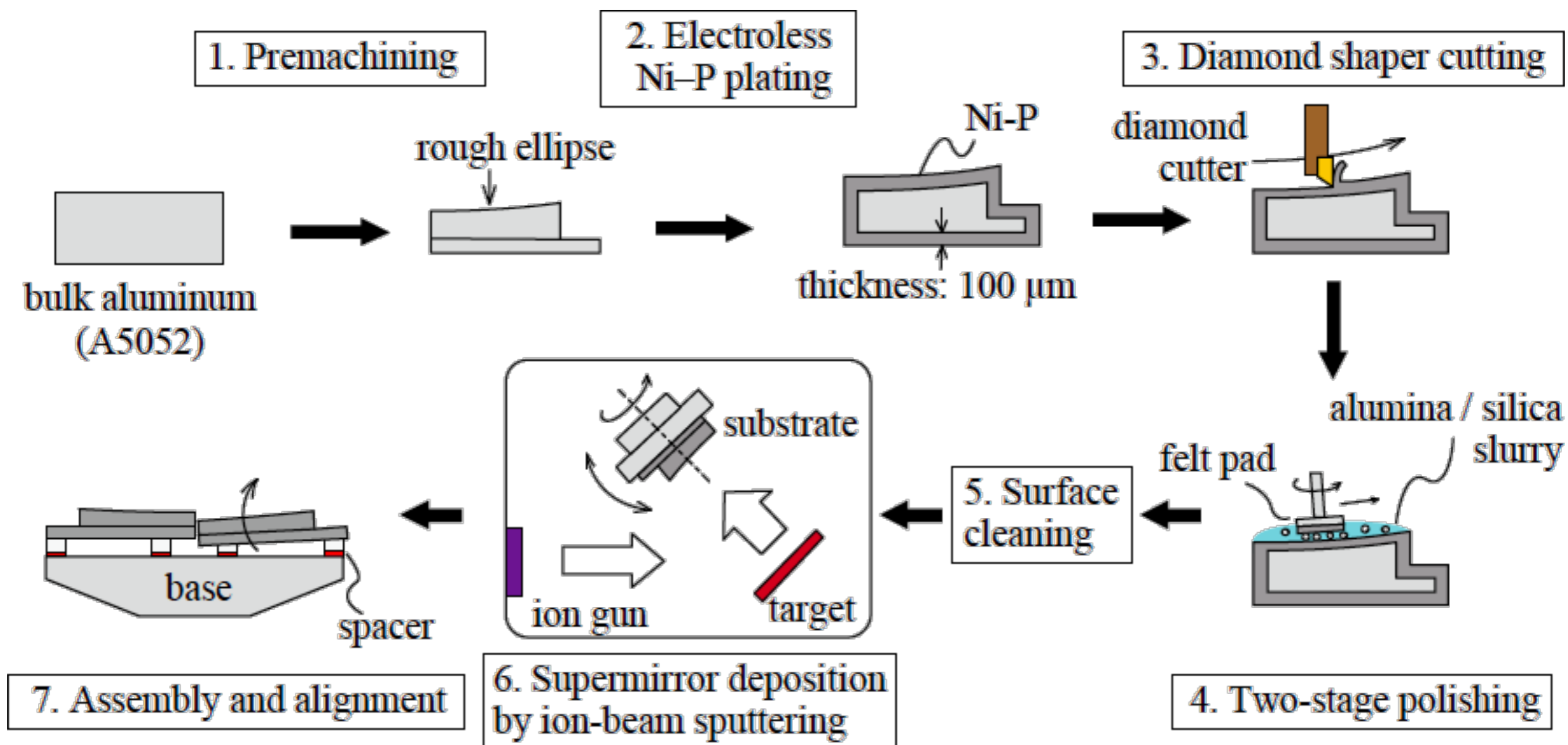
Ni-P plated substrate

kinematic coupling



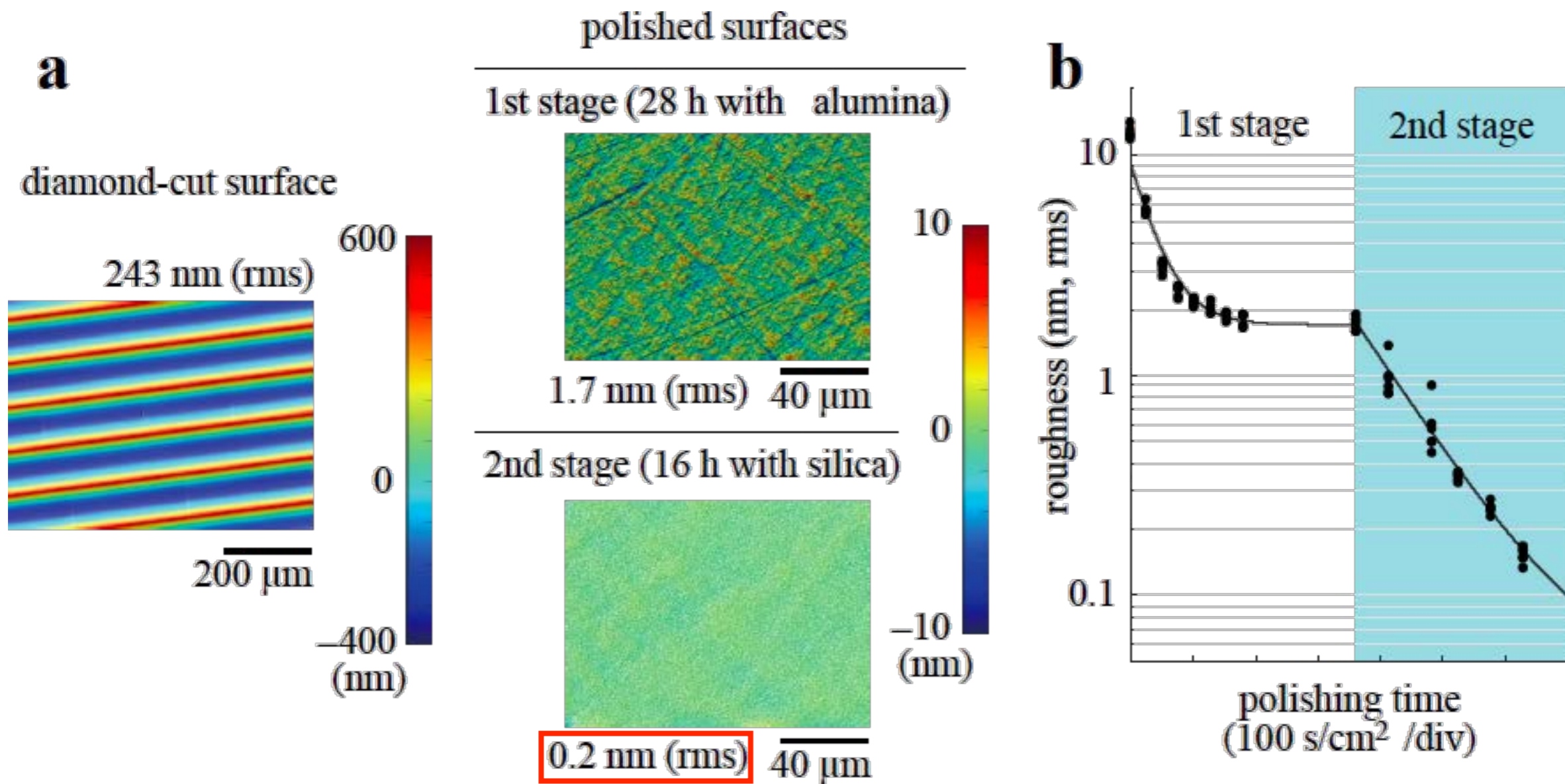
## metal substrate super mirrors (MSSM)

# fabrication of metal substrates

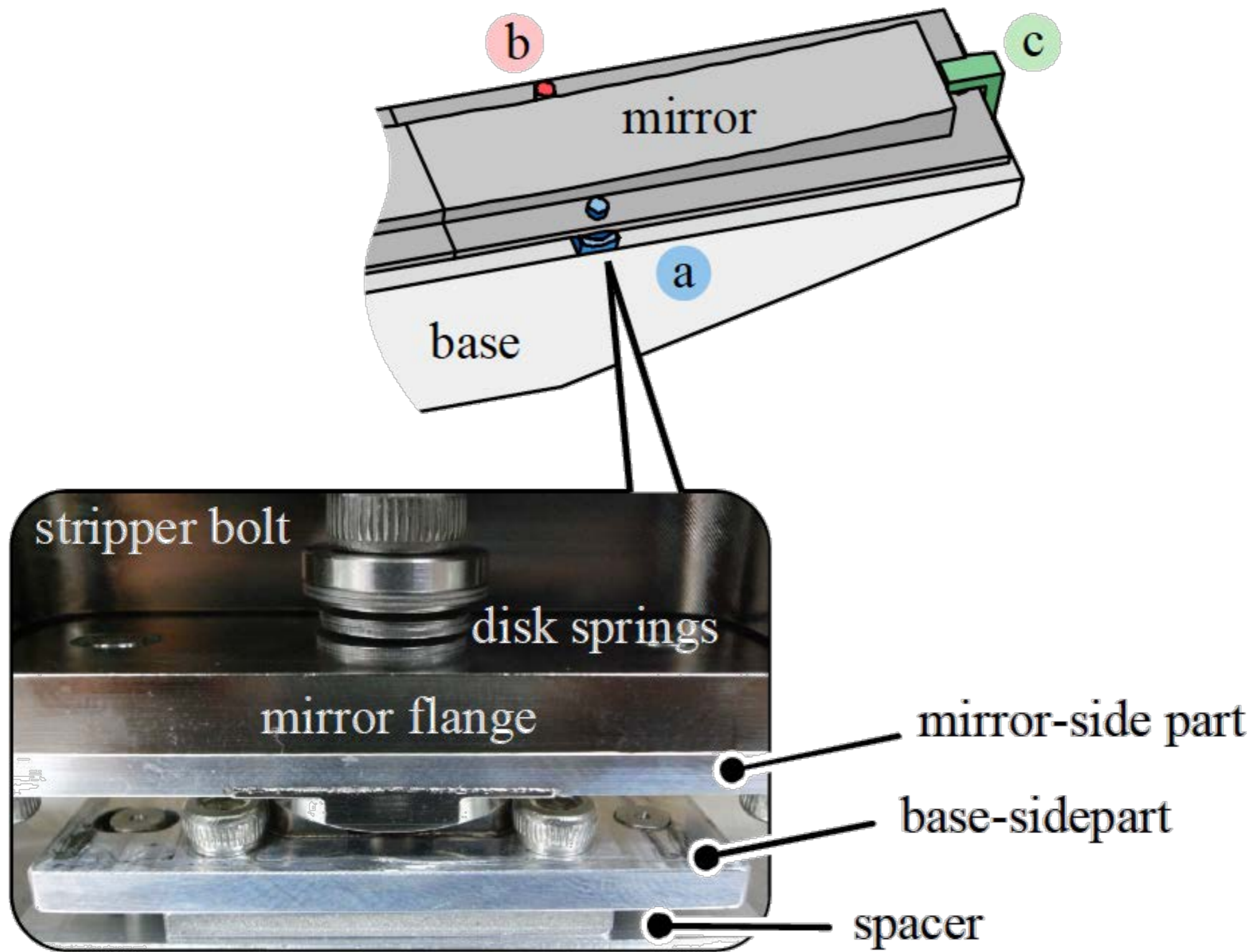




# polishing of Ni-P plated surface

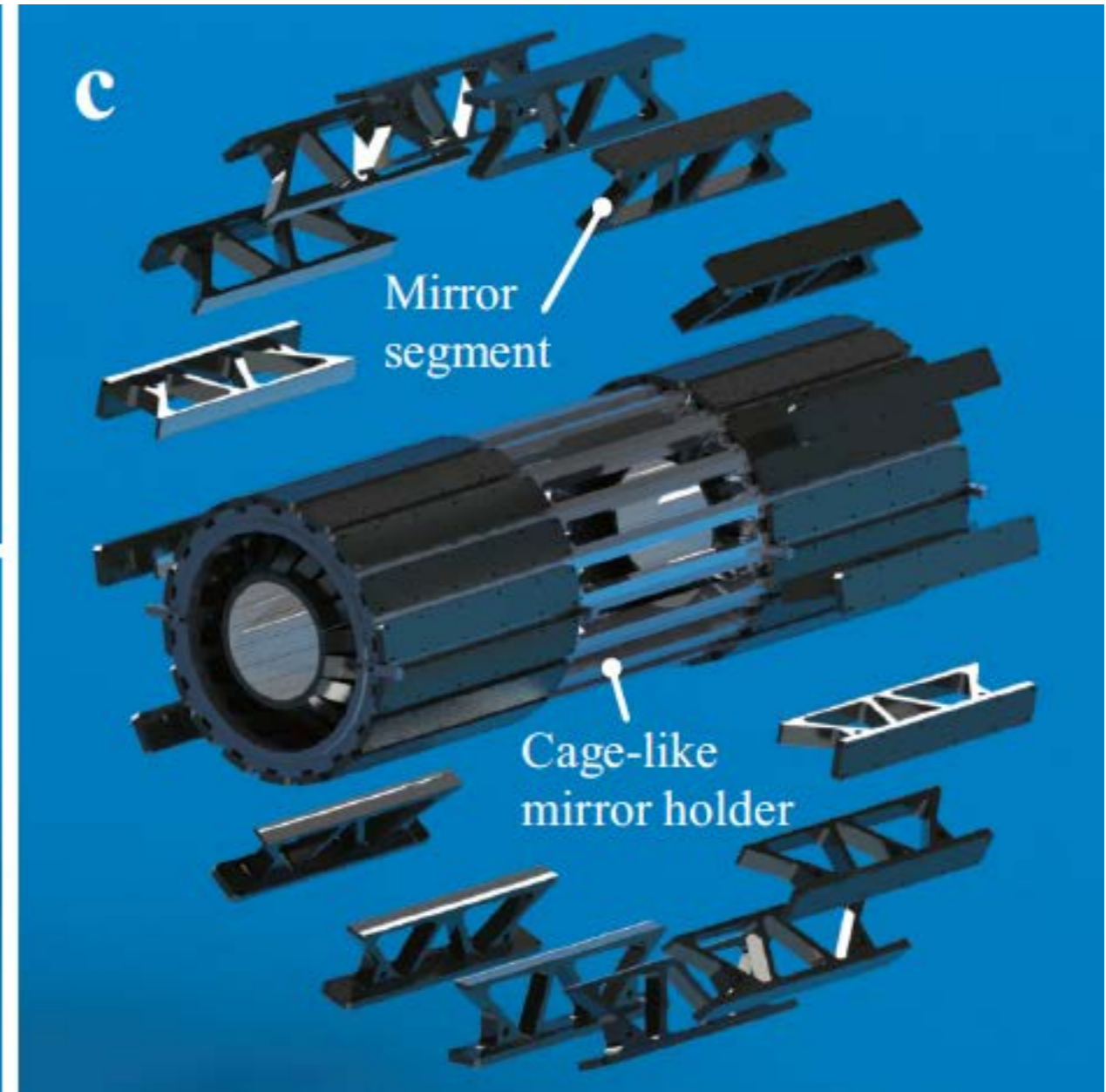
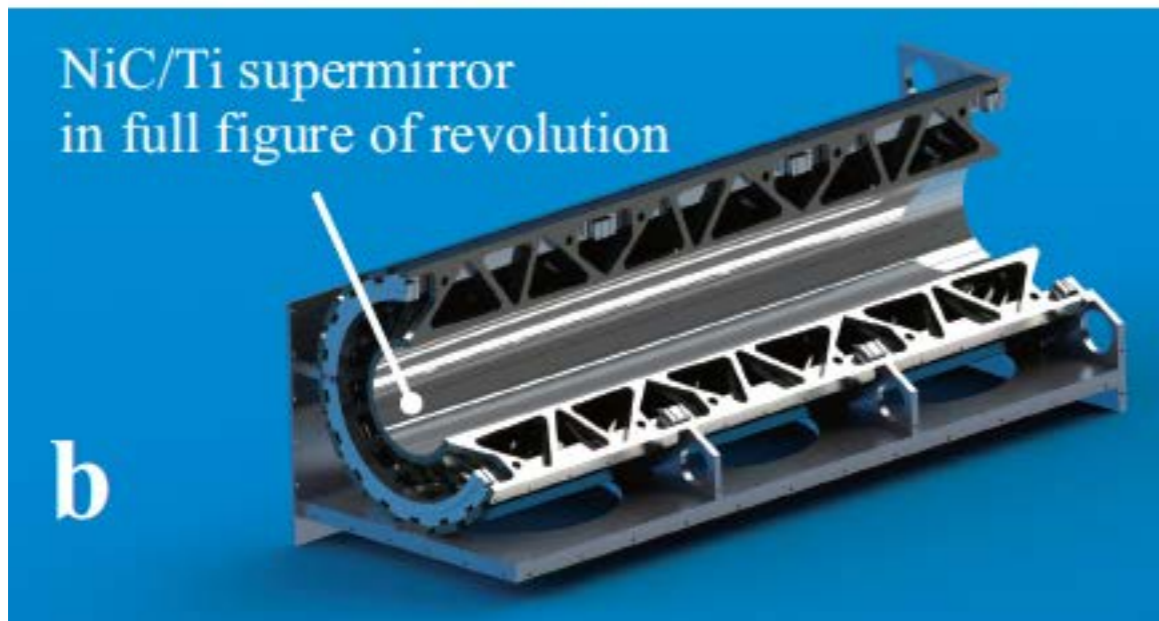
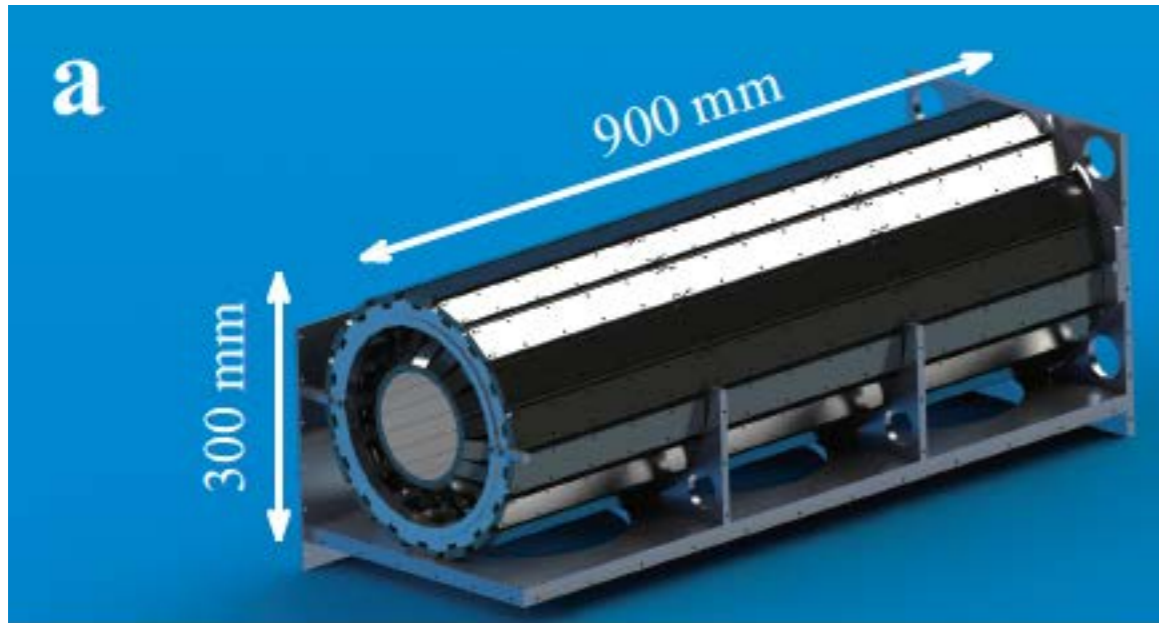


# precision assembling metal-substrate mirrors





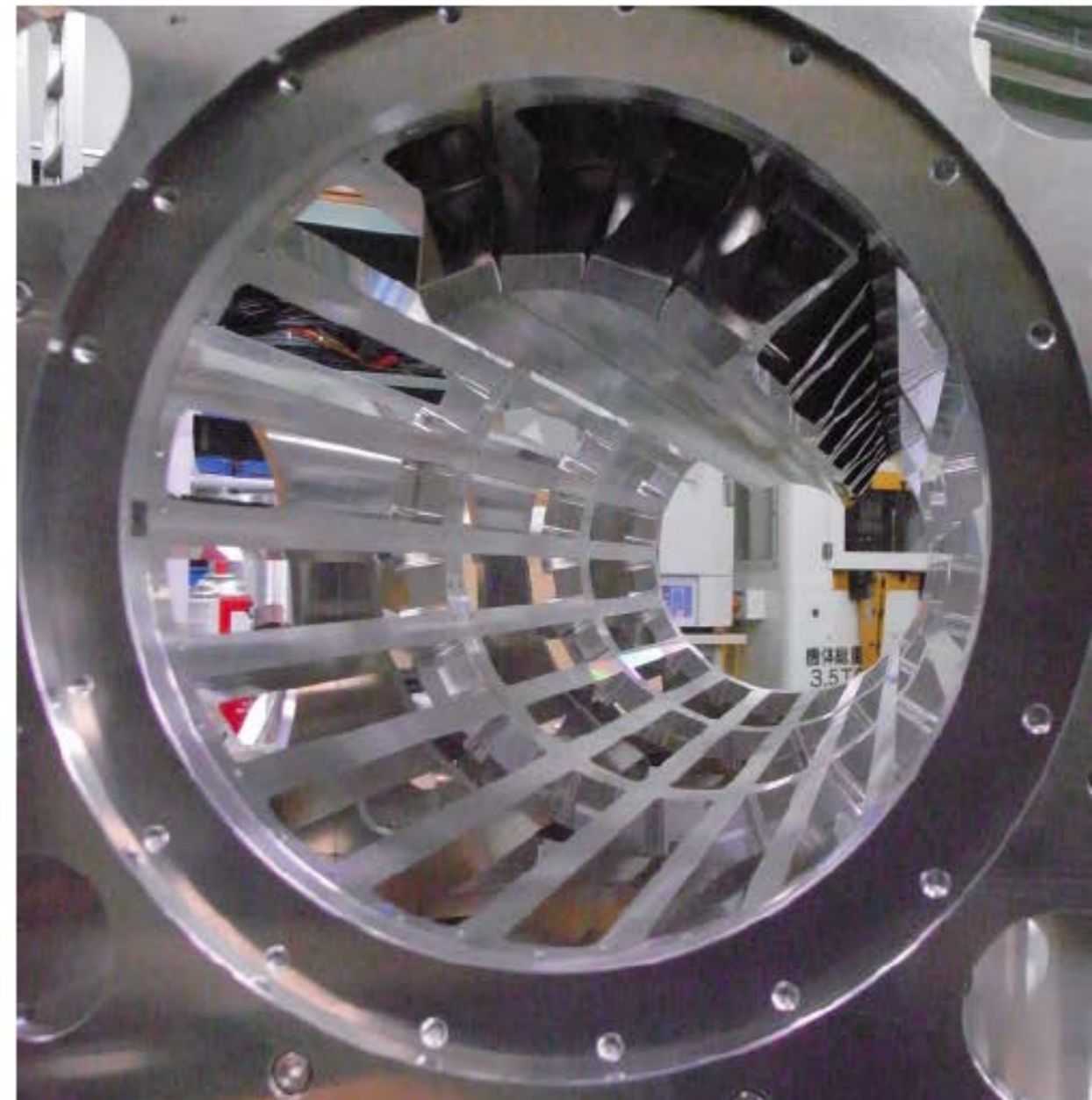
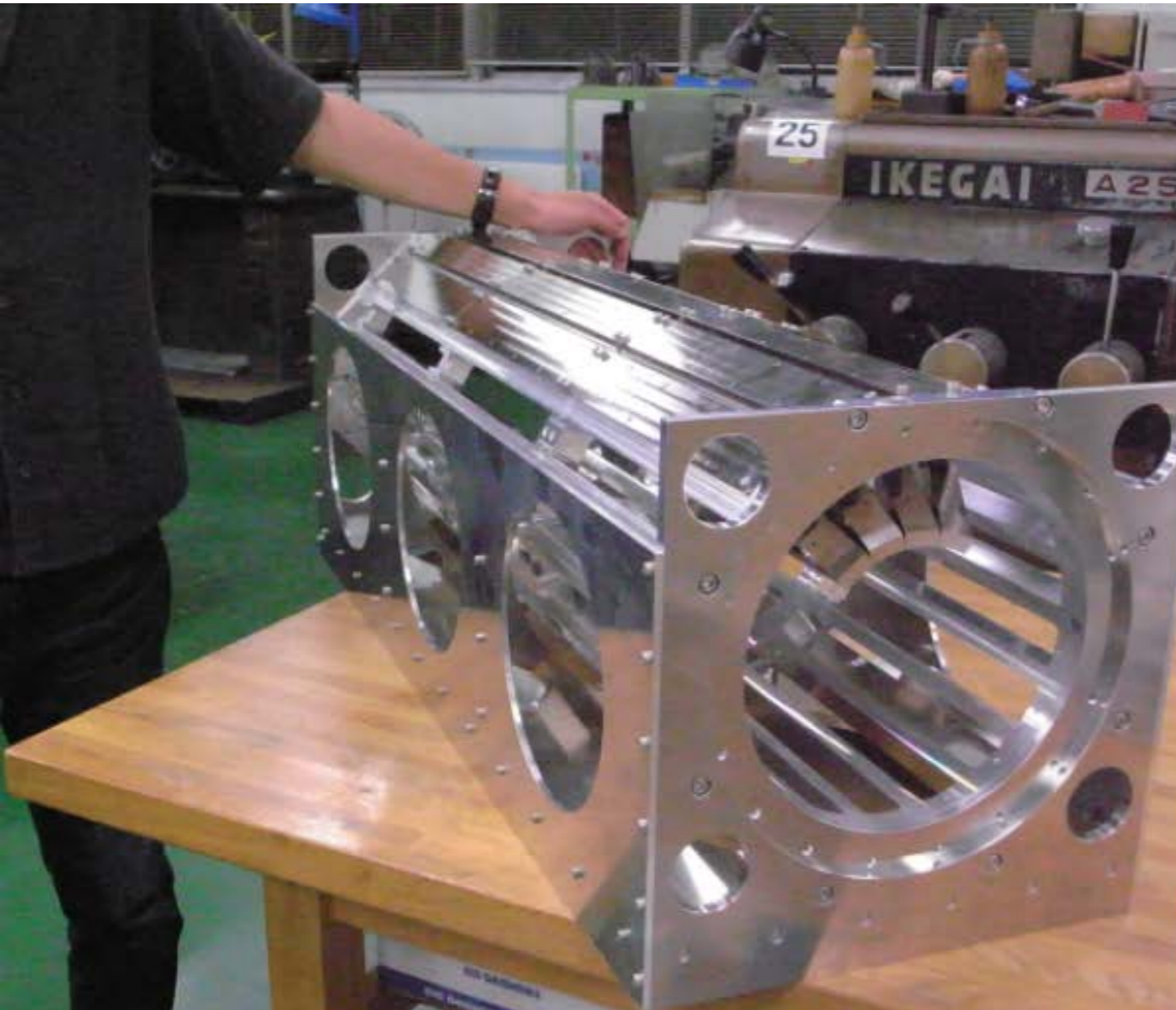
# reflective focusing unit



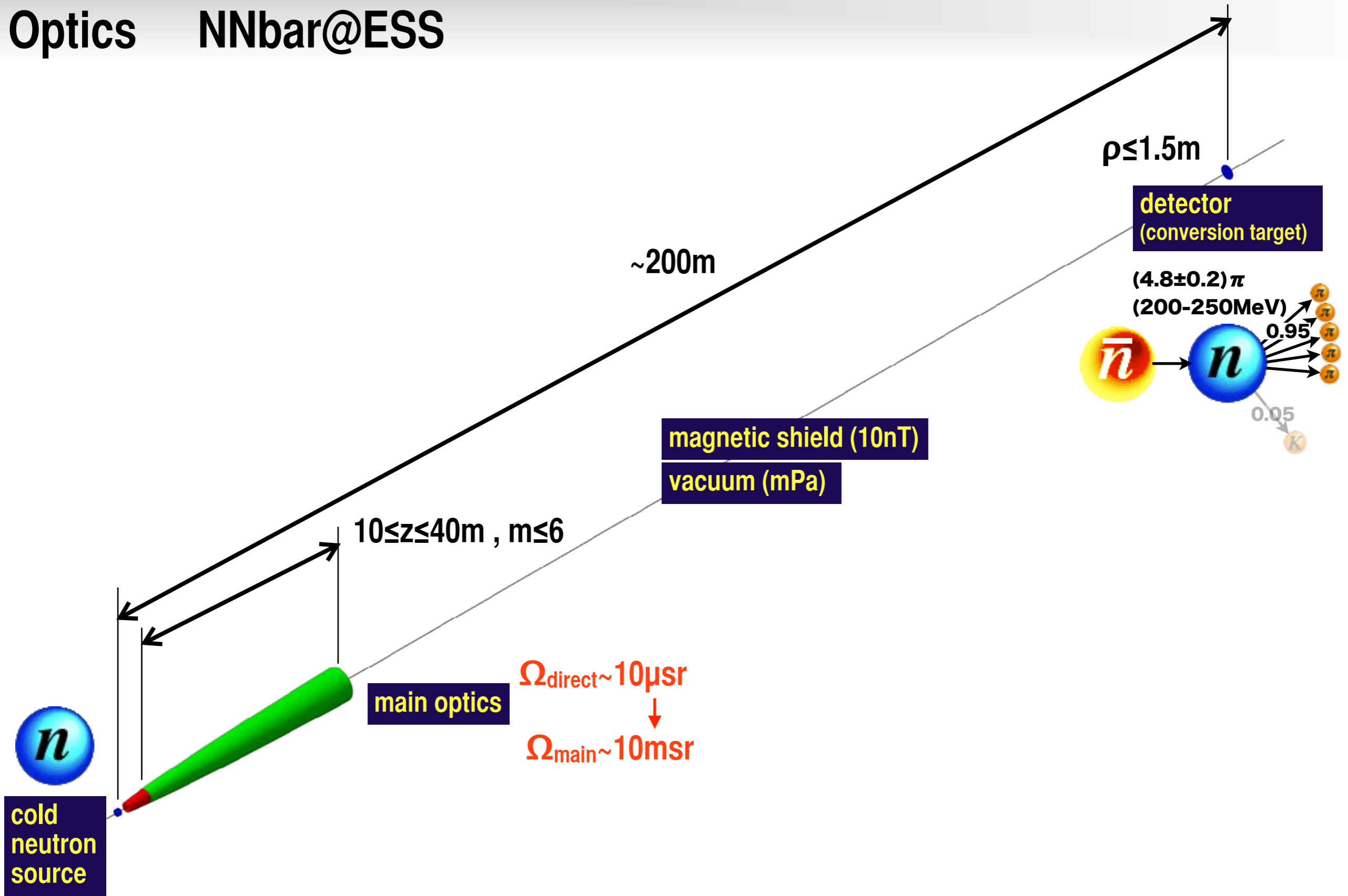
**fully metallic -> radiation-hard**



# reflective focusing unit

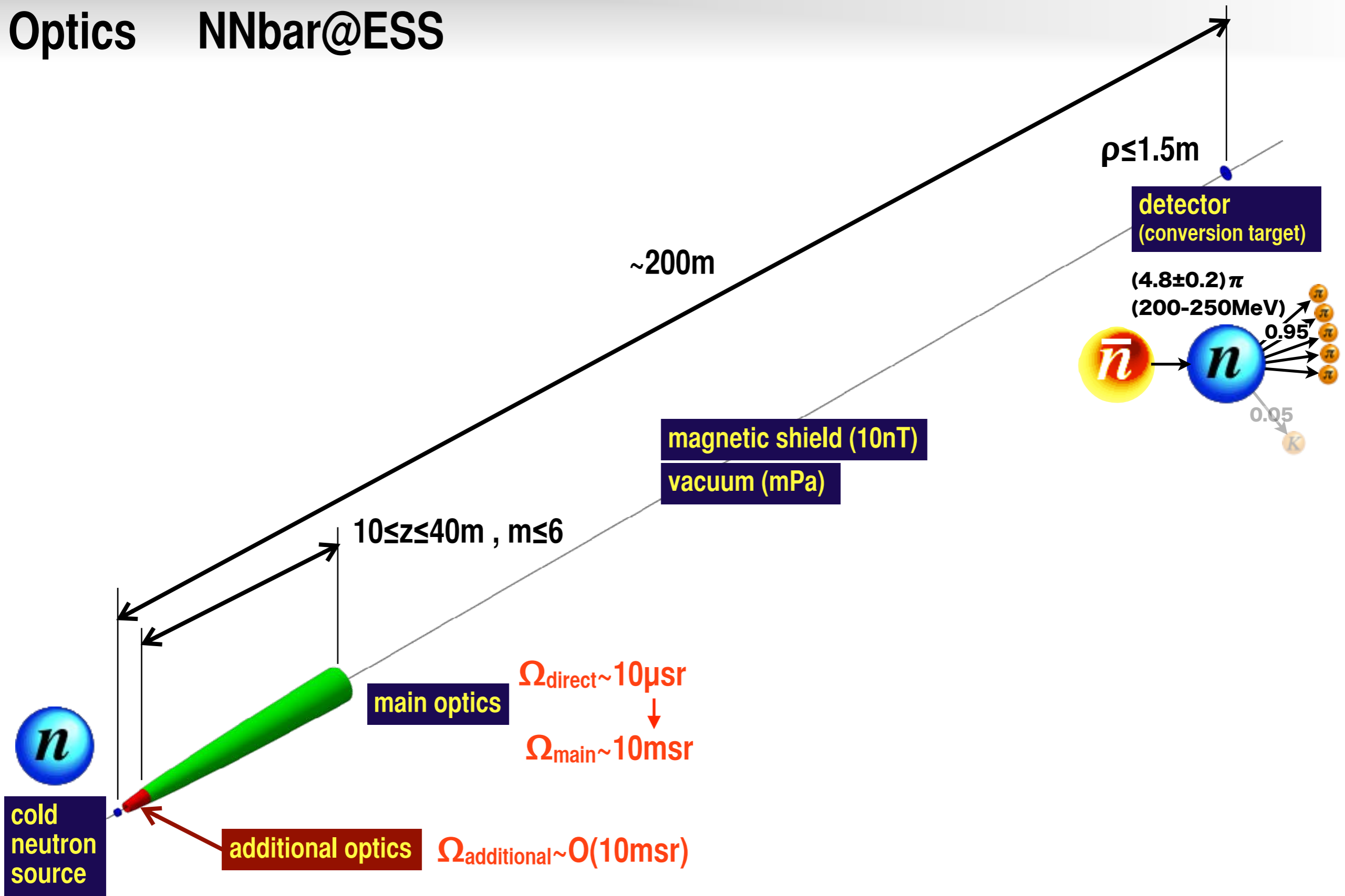


# Optics NNbar@ESS



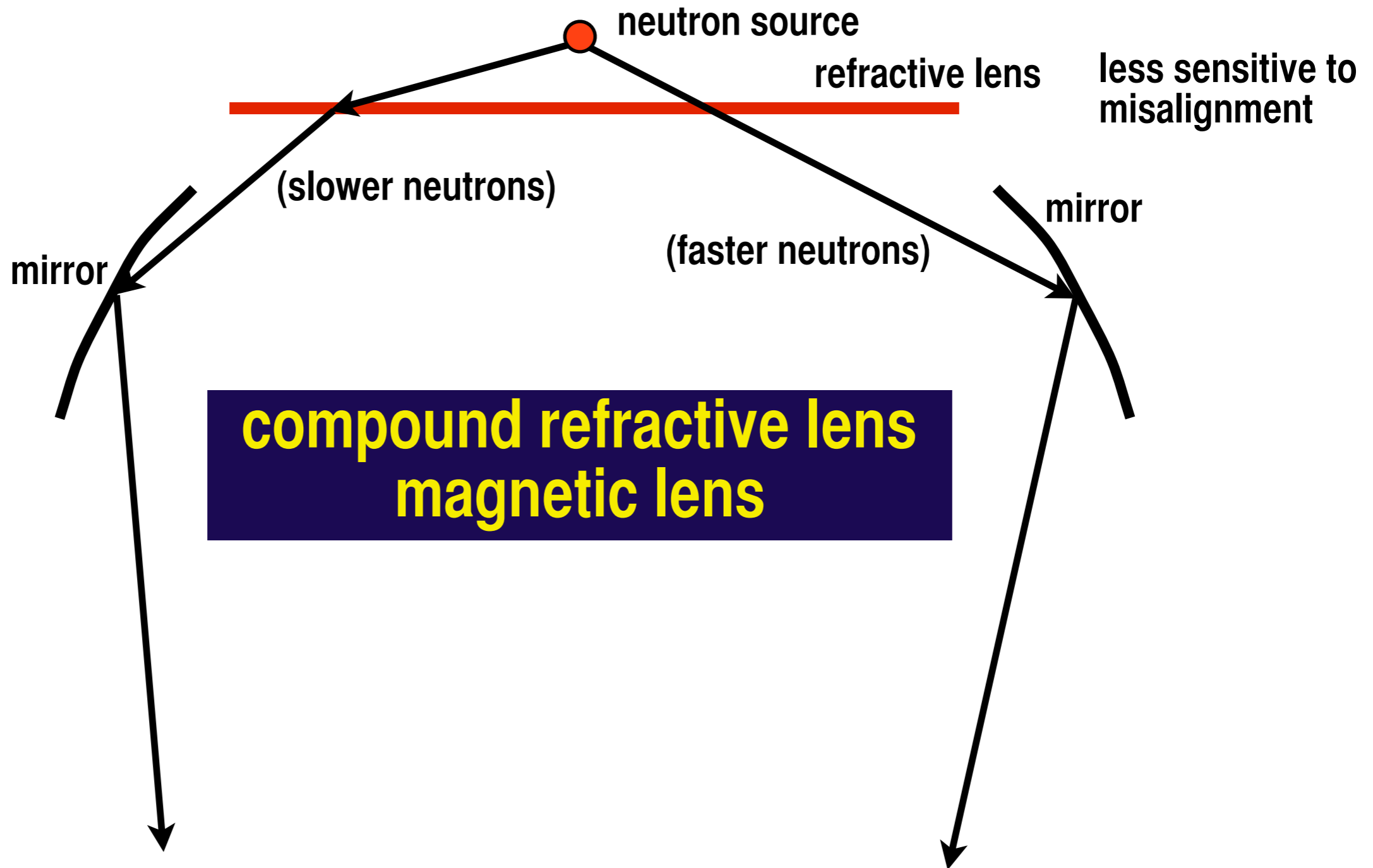


# Optics NNbar@ESS

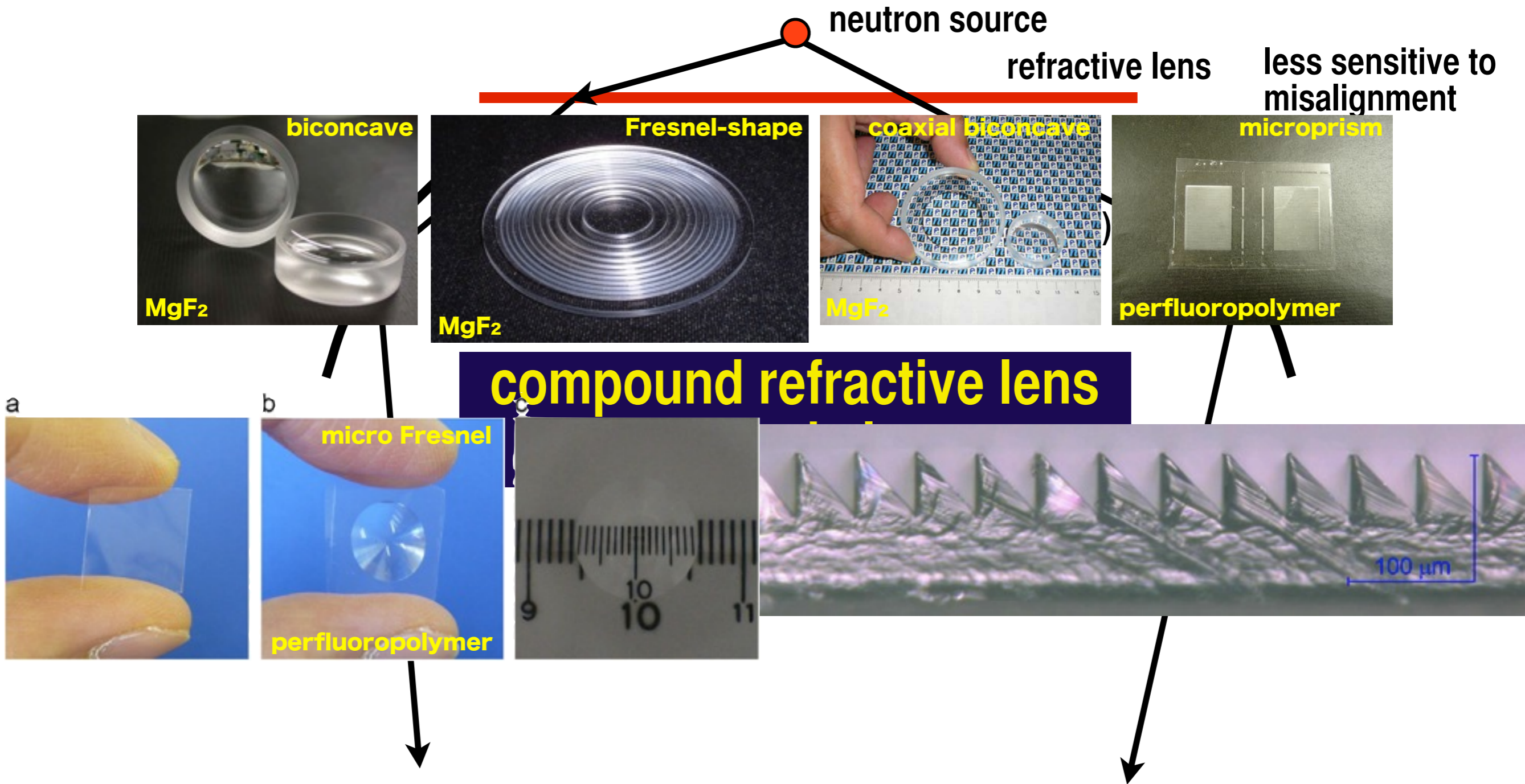




# Refractive Lens for Enlarging Effective Acceptance



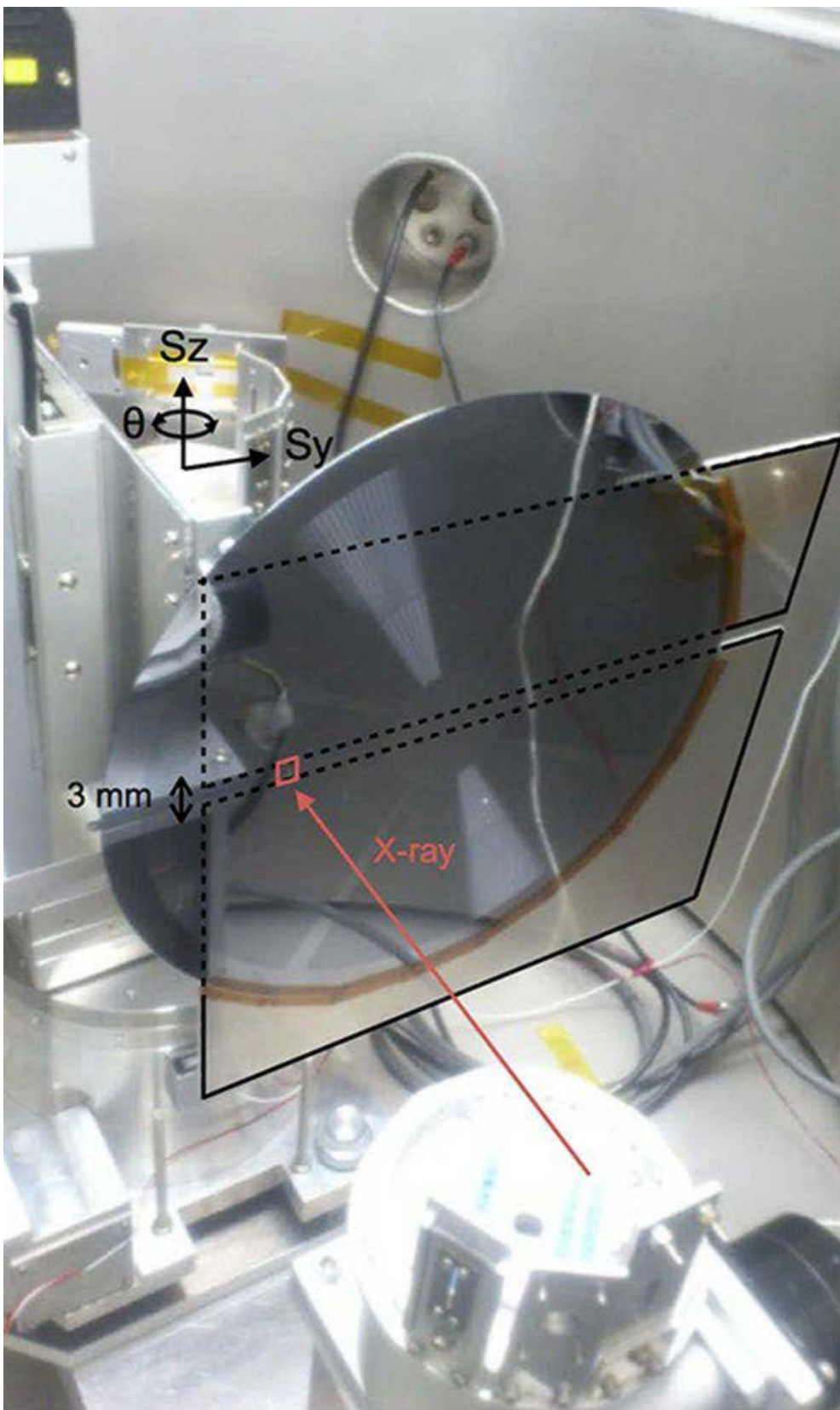
# Refractive Lens for Enlarging Effective Acceptance





# MEMS X-ray Lens

K.Ishikawa, Y.Ezoe et al., DOI 10.1007/s00542-016-2980-6 Microsyst. Technol. (2016)



0) Silicon wafer

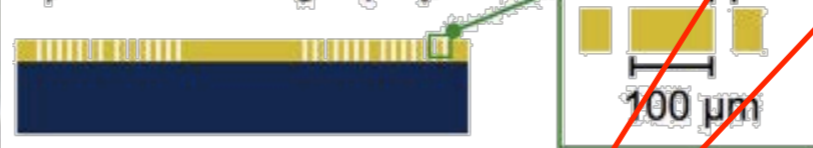
~300 mm (12 inch)



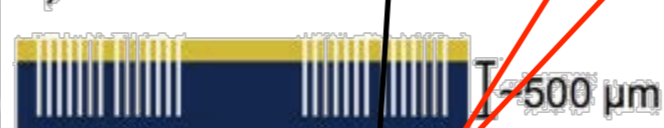
1) Deposit photoresist



2) Photolithography

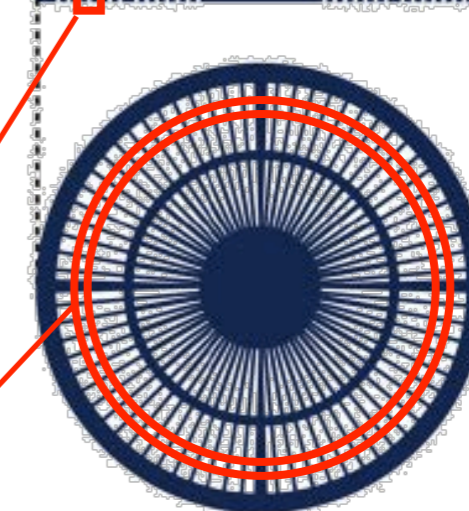


3) DRIE

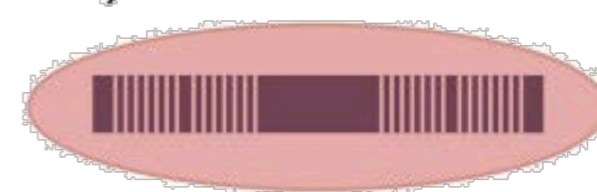


4) Grinding and polishing of backside

~400  $\mu\text{m}$

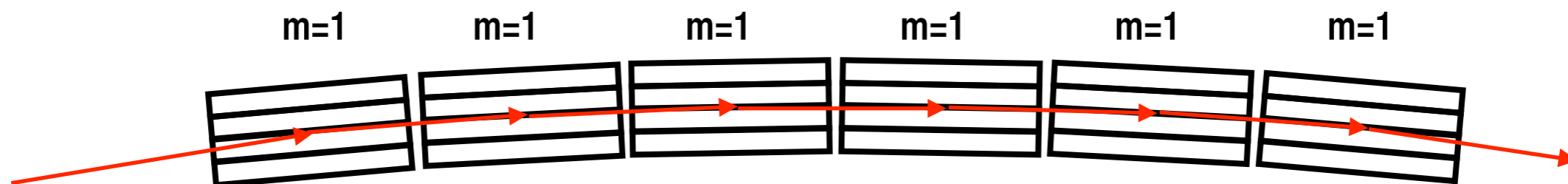


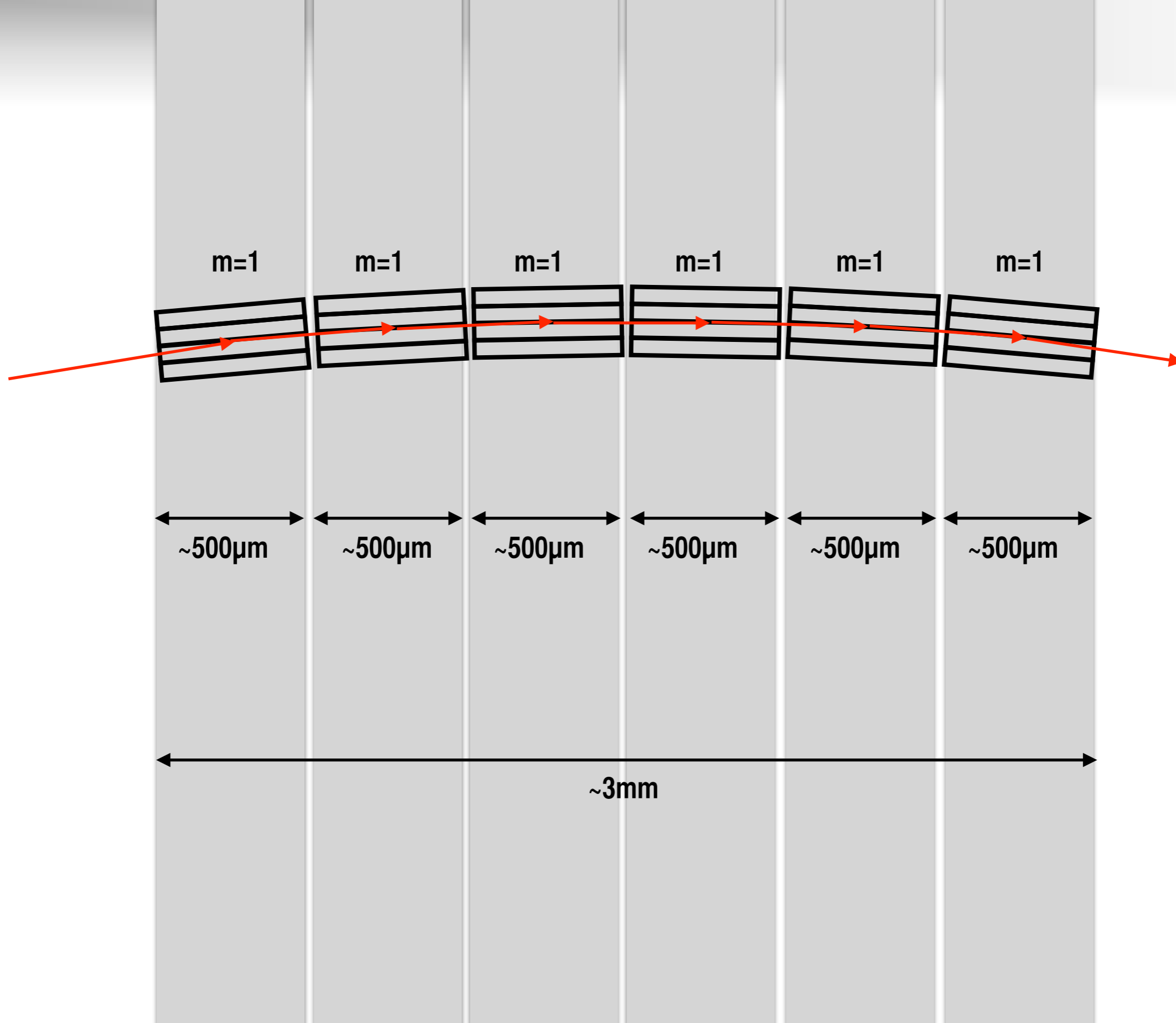
5) Anneal

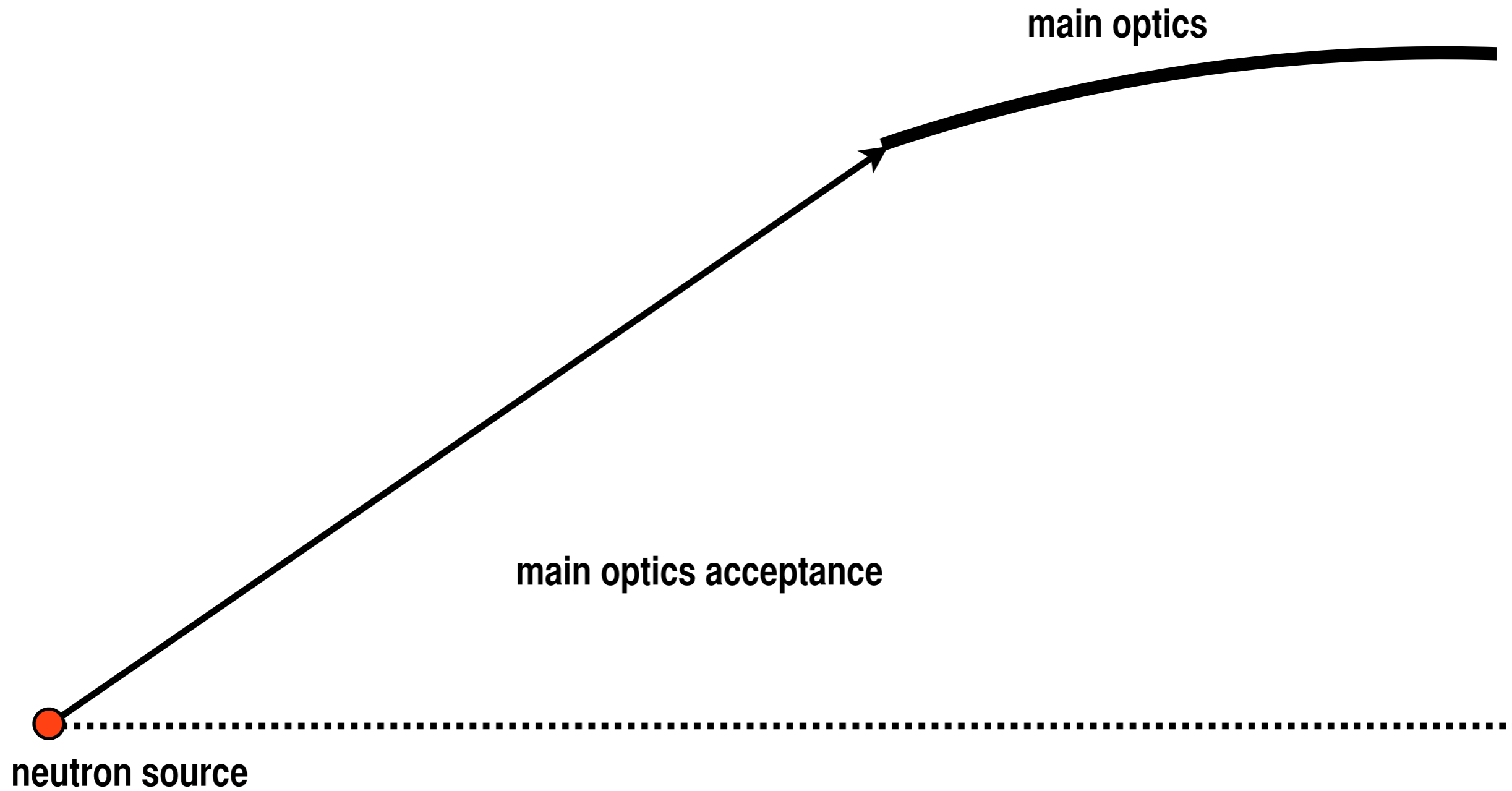


aspect ratio ~ 1:20  
coating demonstrated  
nickel ( $m=1$ )

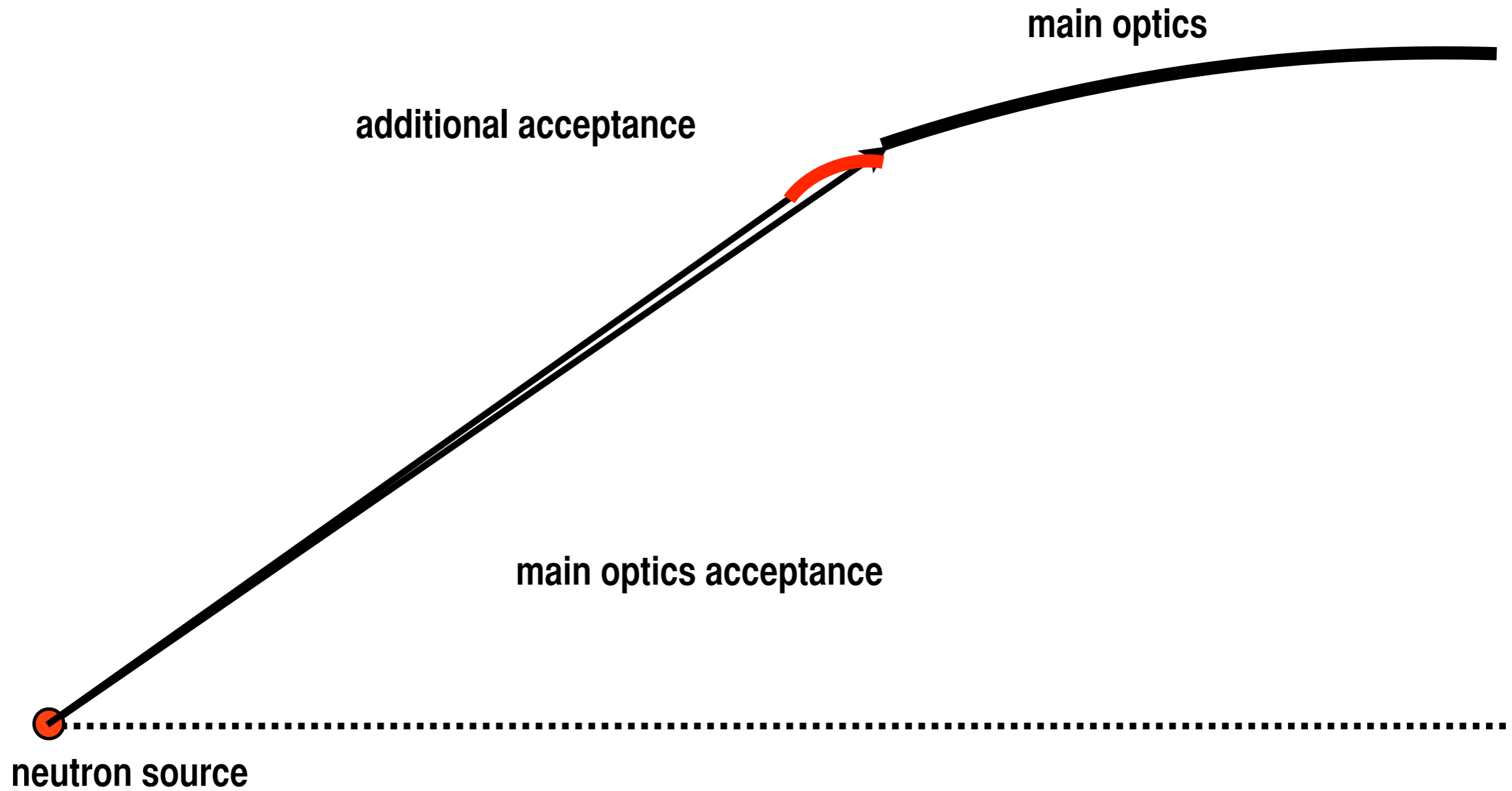


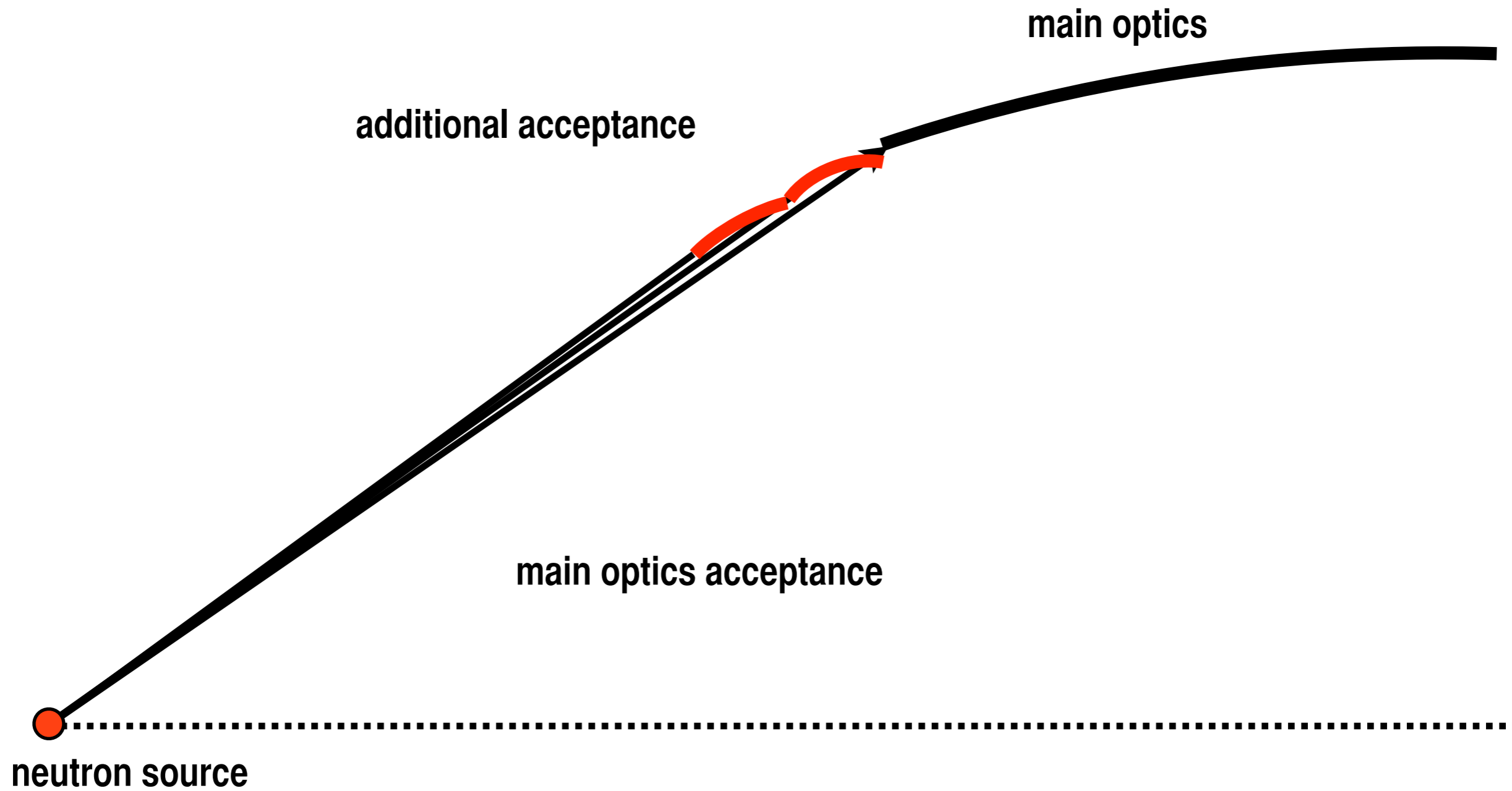


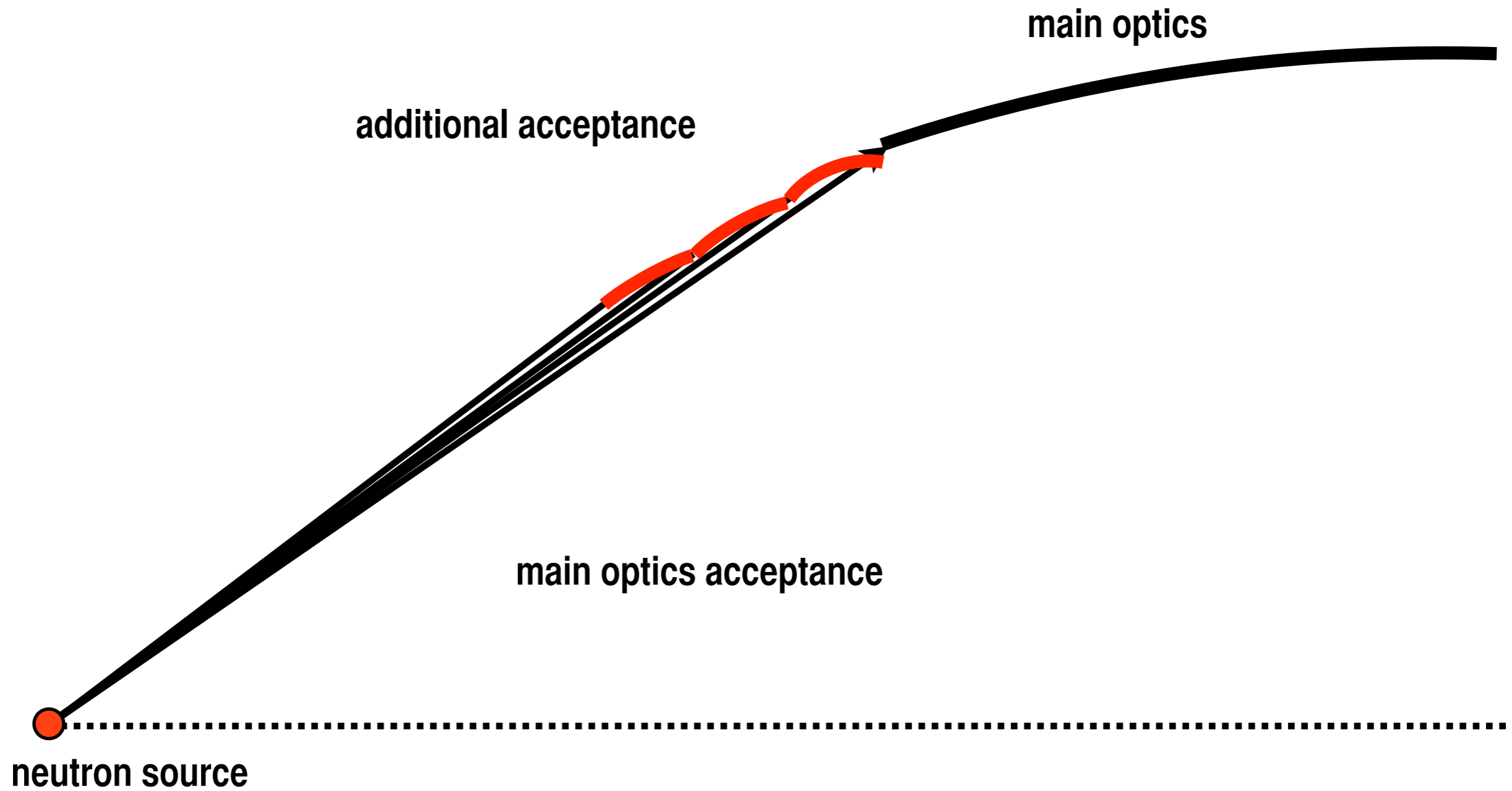














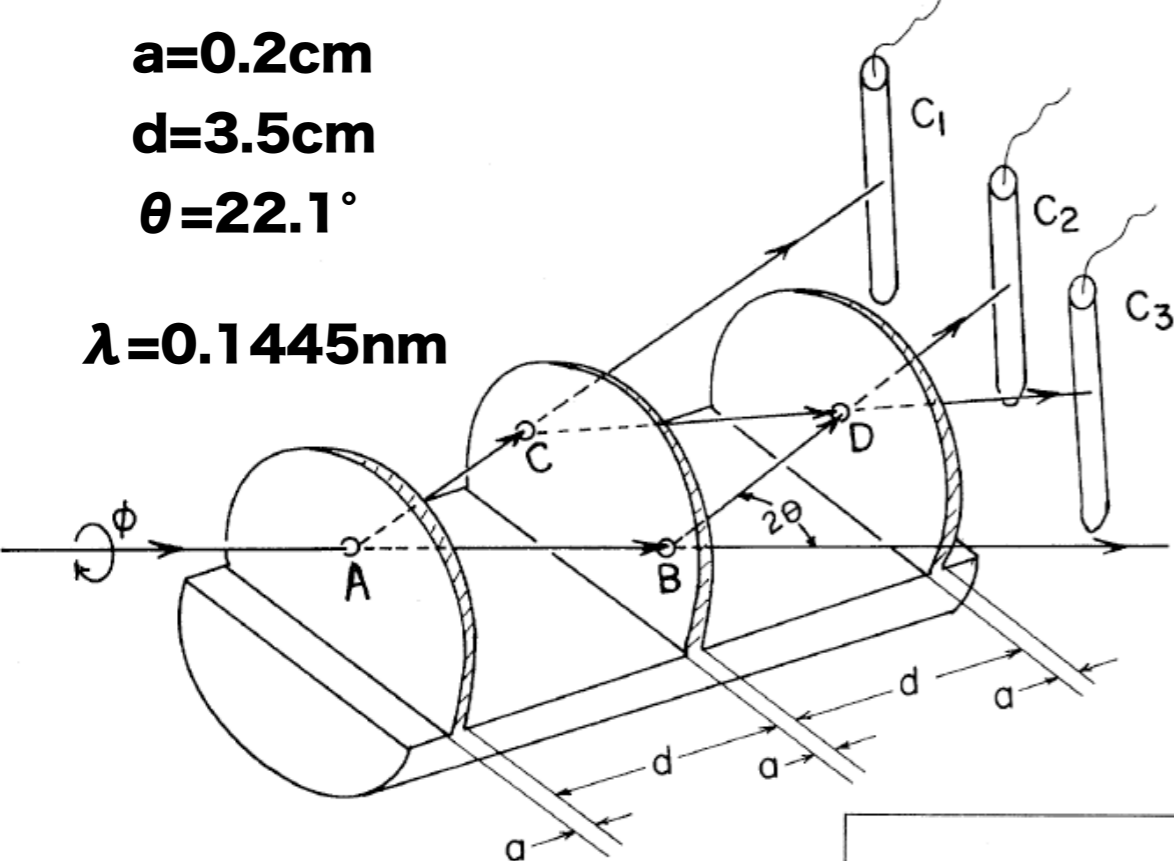
# Neutron Interferometry

# Neutron Phase induced by Earth's Gravity

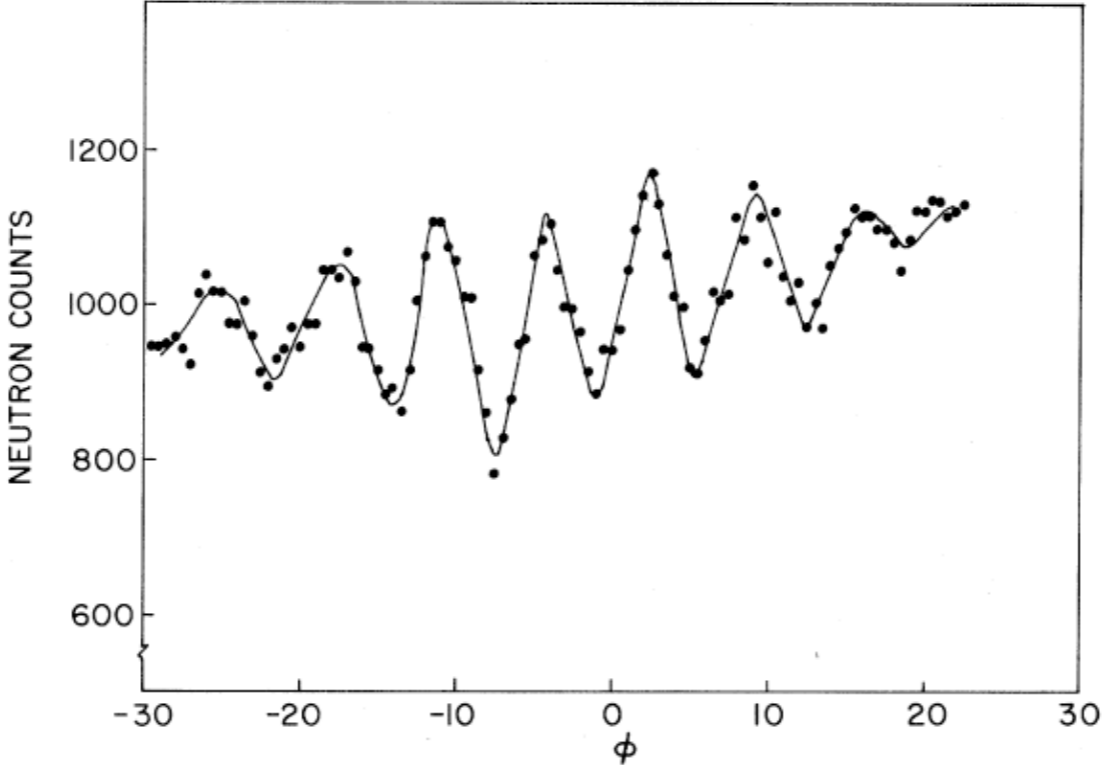
Collela, Overhauser, Werner, Phys. Rev. Lett. 34 (1975) 1472

$a=0.2\text{cm}$   
 $d=3.5\text{cm}$   
 $\theta=22.1^\circ$

$\lambda=0.1445\text{nm}$



## COW experiment



# Neutron Phase induced by Earth's Gravity

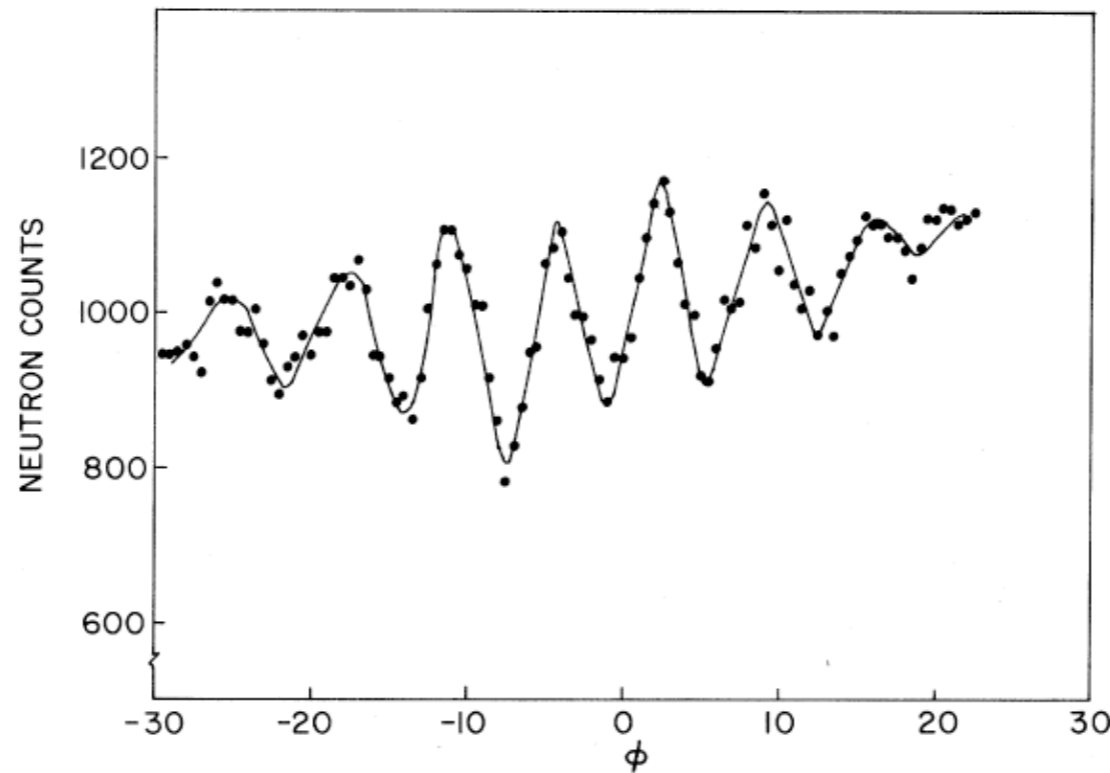
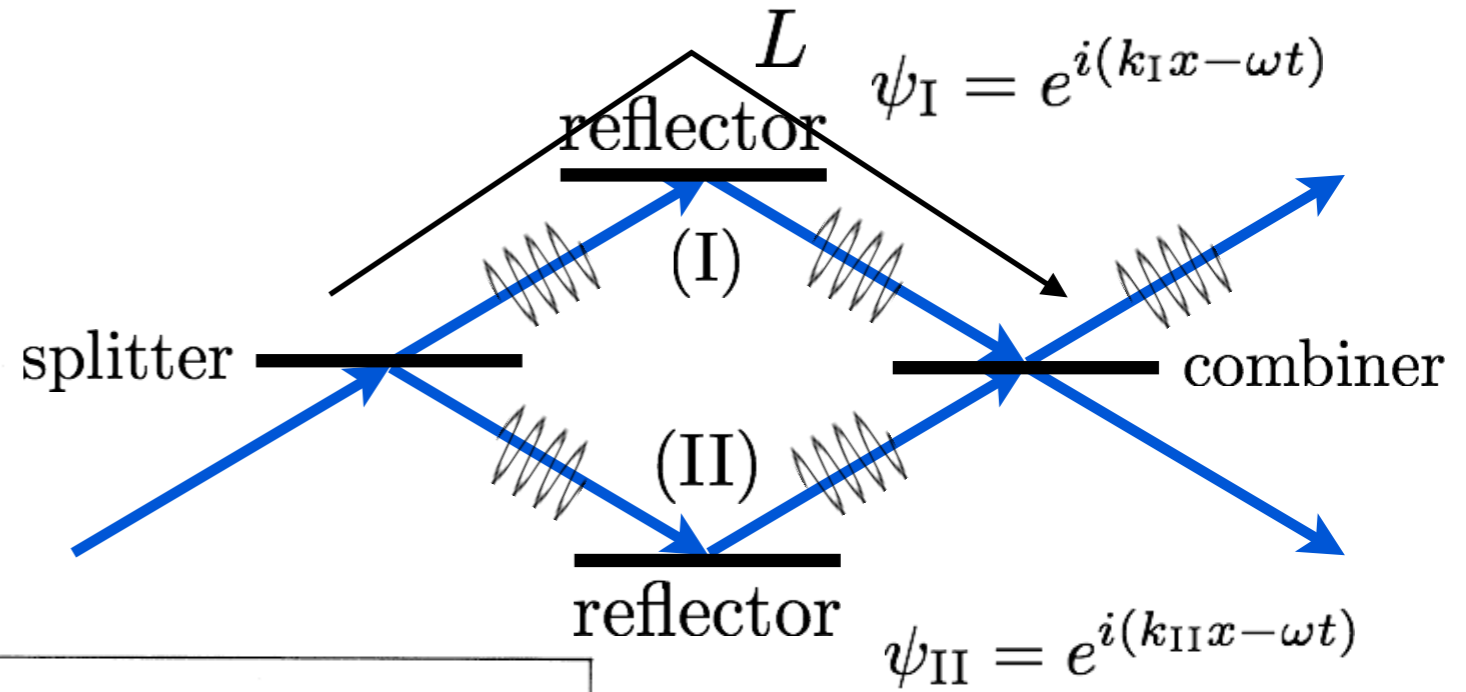
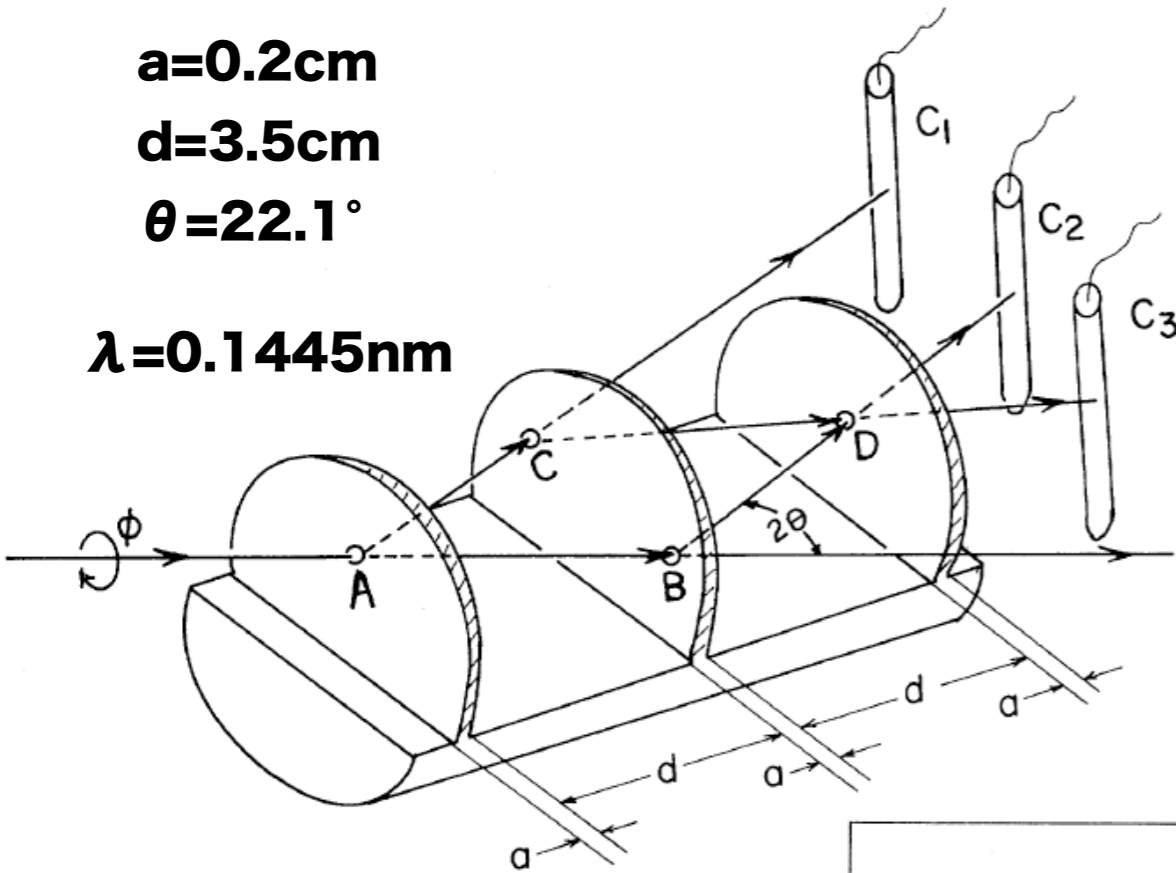
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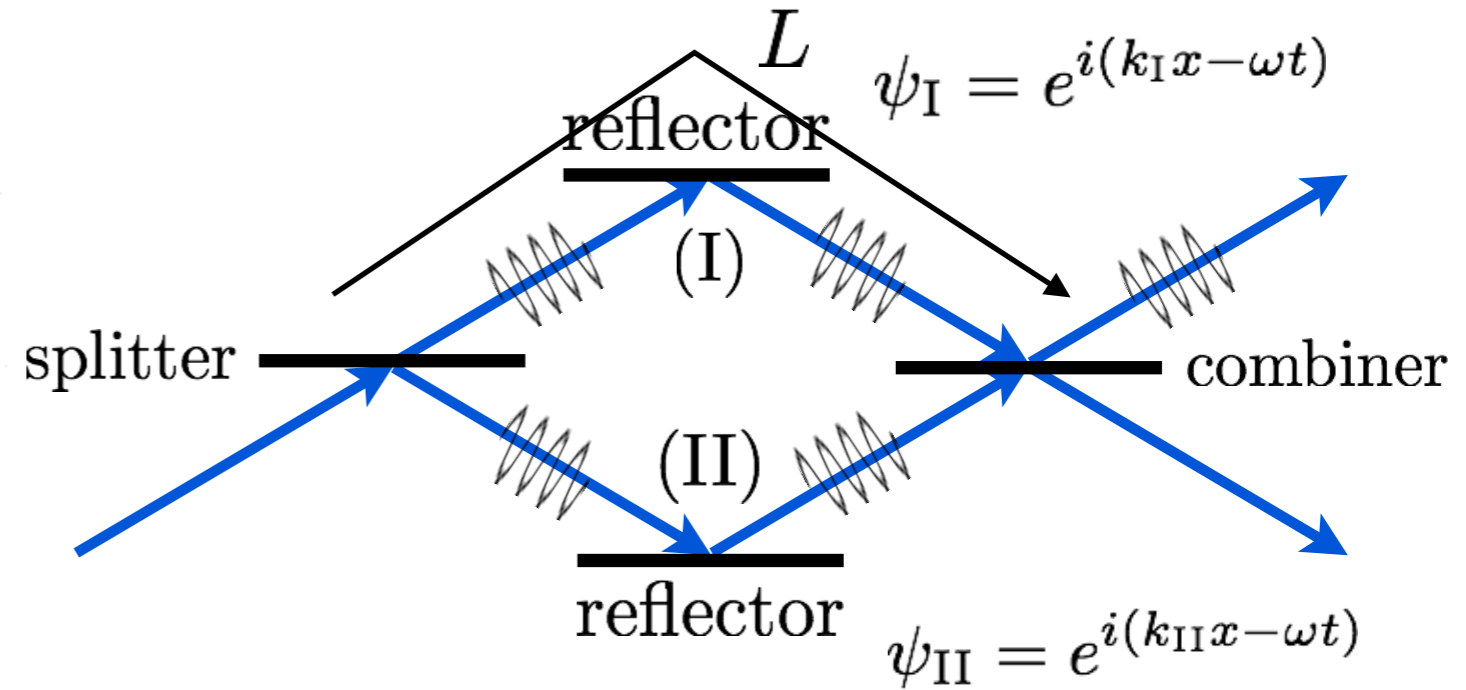
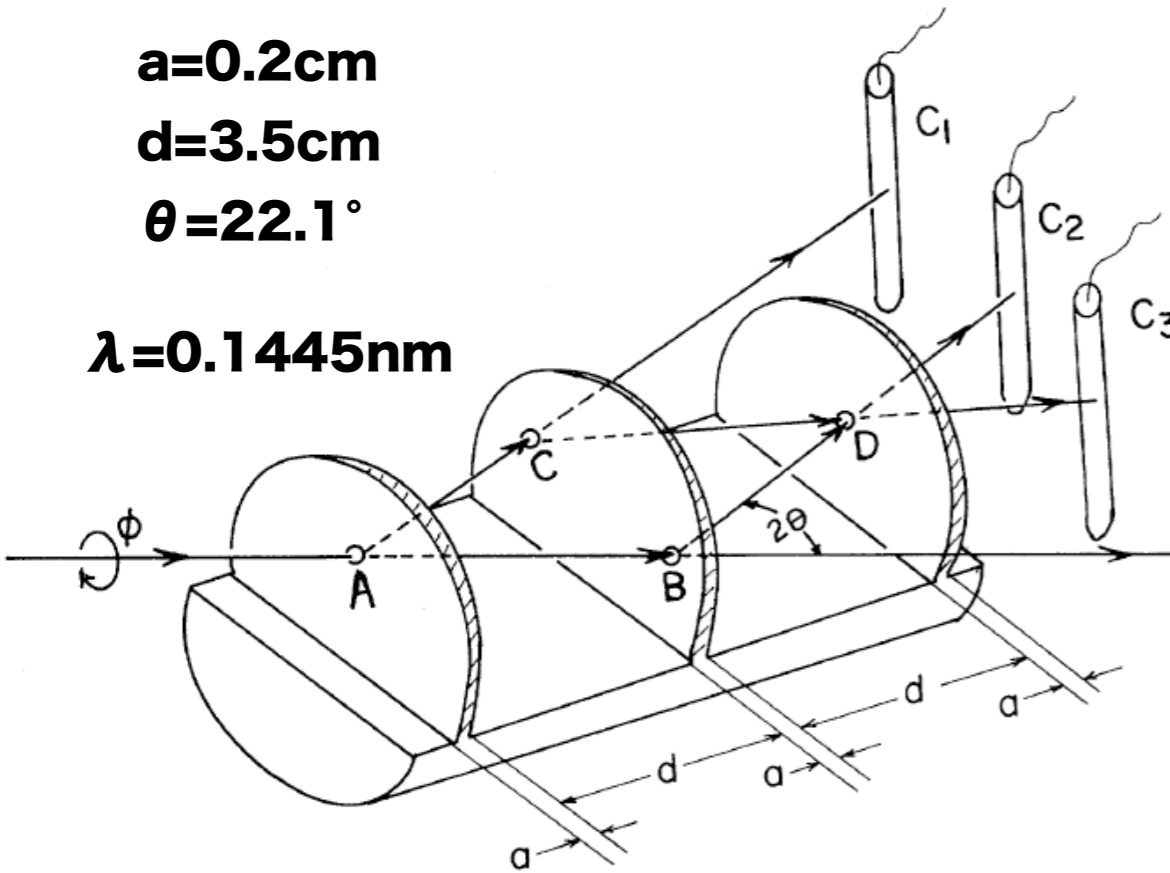
Collela, Overhauser, Werner, Phys. Rev. Lett. 34 (1975) 1472

$a=0.2\text{cm}$

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$\theta=22.1^\circ$

$\lambda=0.1445\text{nm}$



$$k_I = \frac{\sqrt{2m_n(E_0 + U)}}{\hbar}$$

$$\phi_I = k_I L$$

$$k_{II} = \frac{\sqrt{2m_n(E_0 + U + \Delta U)}}{\hbar}$$

$$\phi_{II} = k_{II} L$$

# Neutron Phase induced by Earth's Gravity

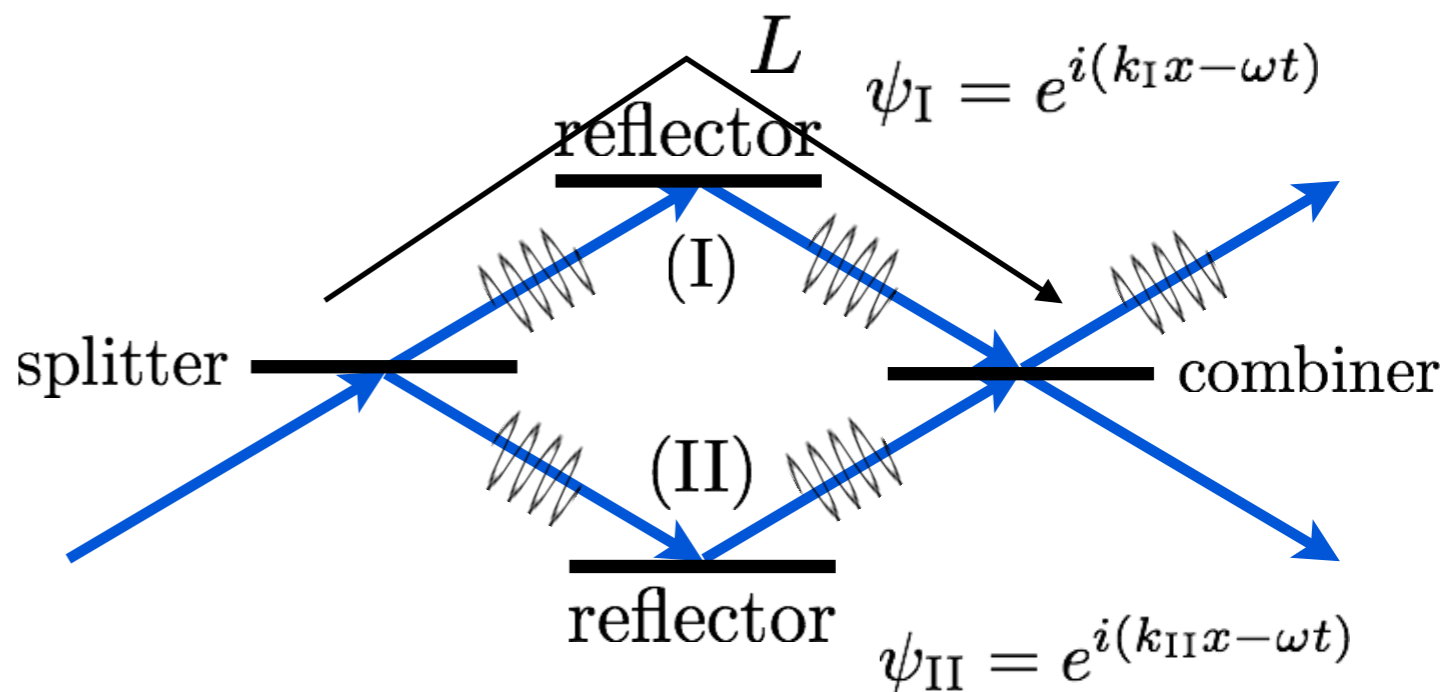
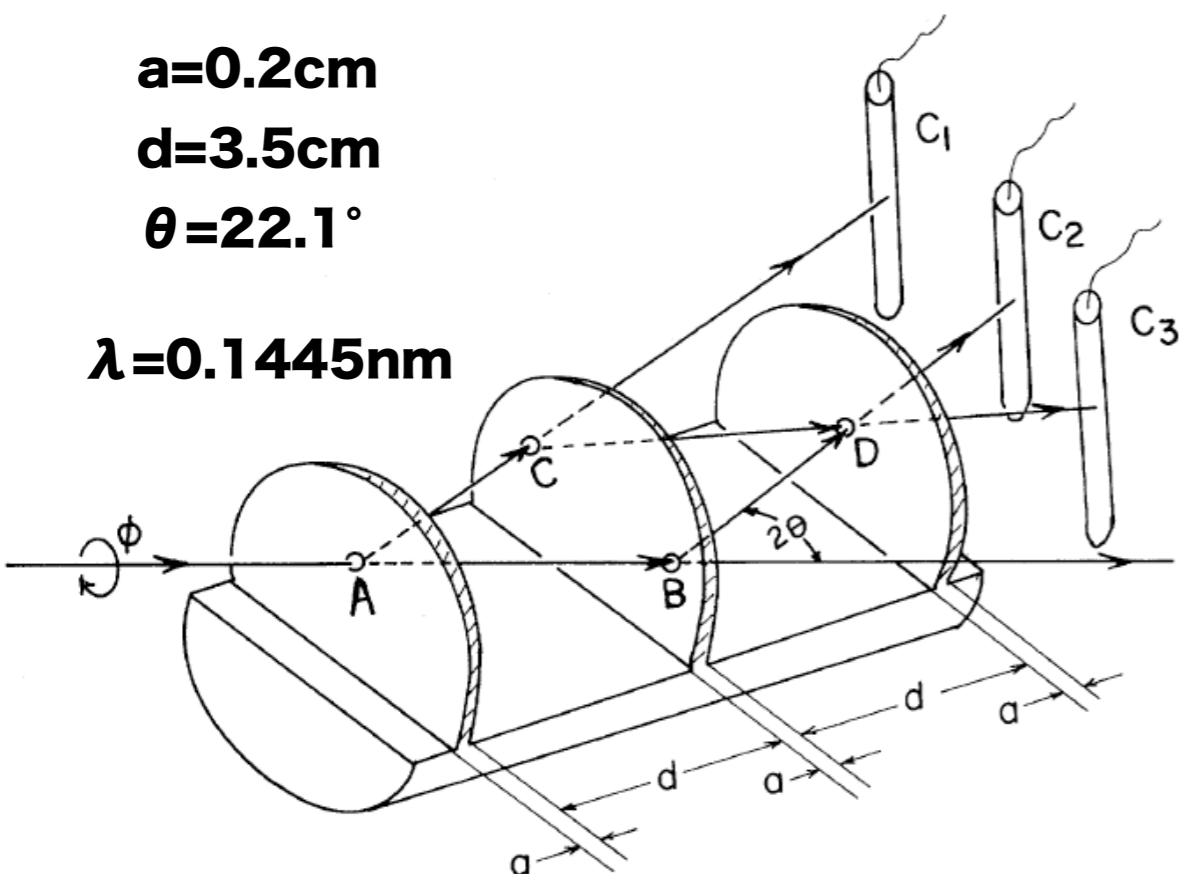
Collela, Overhauser, Werner, Phys. Rev. Lett. 34 (1975) 1472

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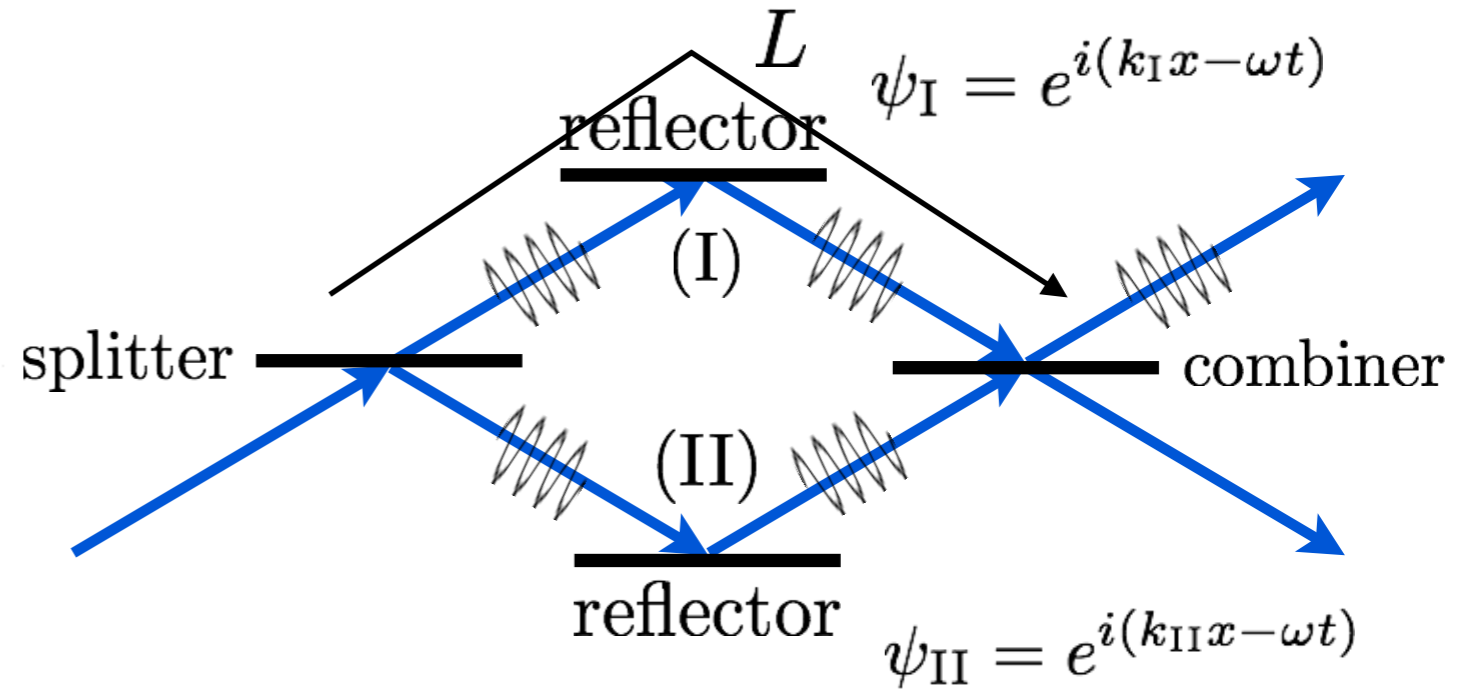
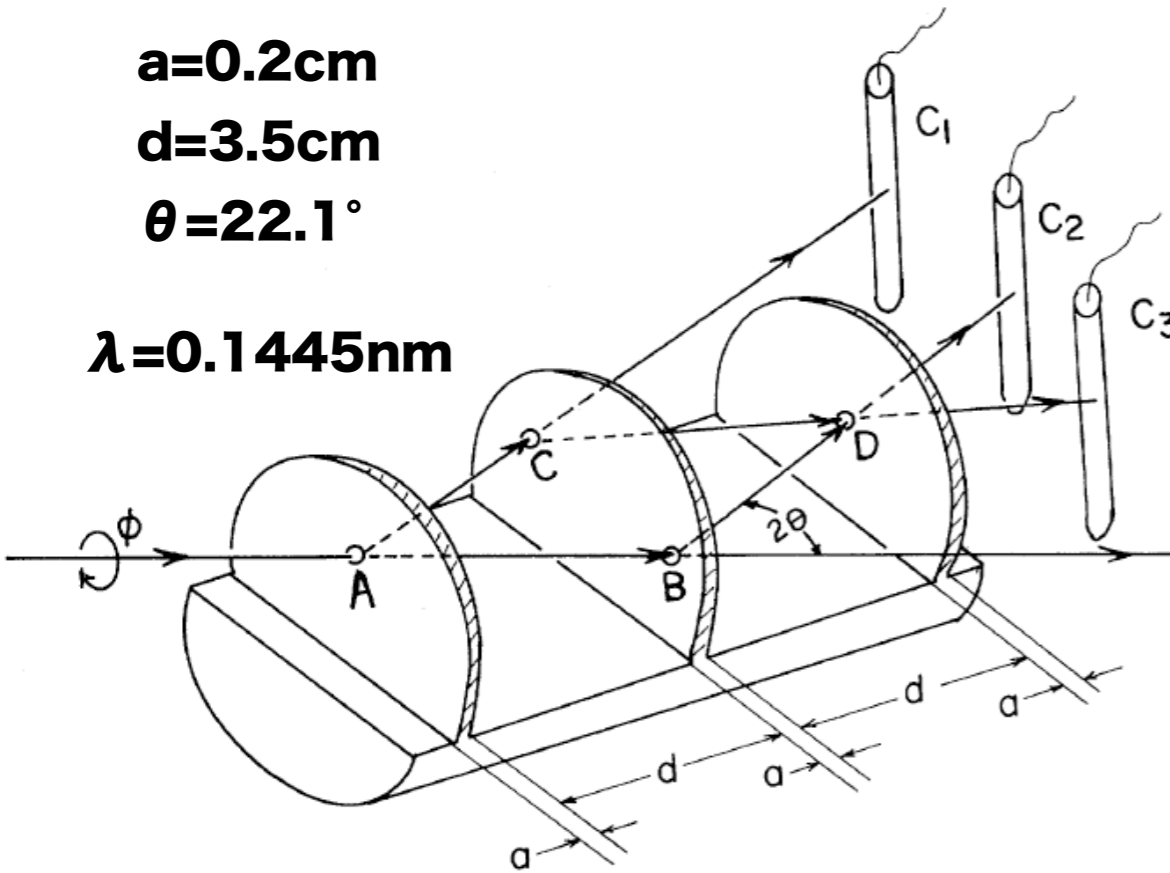
$$\Delta\phi = \phi_{II} - \phi_I \simeq \sqrt{\frac{m_n c^2}{2E}} \frac{L \Delta U}{\hbar c}$$

# Neutron Phase induced by Earth's Gravity

Collela, Overhauser, Werner, Phys. Rev. Lett. 34 (1975) 1472

$a=0.2\text{cm}$   
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$\lambda=0.1445\text{nm}$



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$$\phi_I = k_I L$$

$$k_{II} = \frac{\sqrt{2m_n(E_0 + U + \Delta U)}}{\hbar}$$

$$\phi_{II} = k_{II} L$$

larger interferometer

$$\Delta\phi = \phi_{II} - \phi_I \simeq \sqrt{\frac{m_n c^2 L \Delta U}{2E}} \frac{1}{\hbar c}$$

better statistics

slower neutron



# Neutron Phase induced by Earth's Gravity

Collela, Overhauser, Werner, Phys. Rev. Lett. 34 (1975) 1472

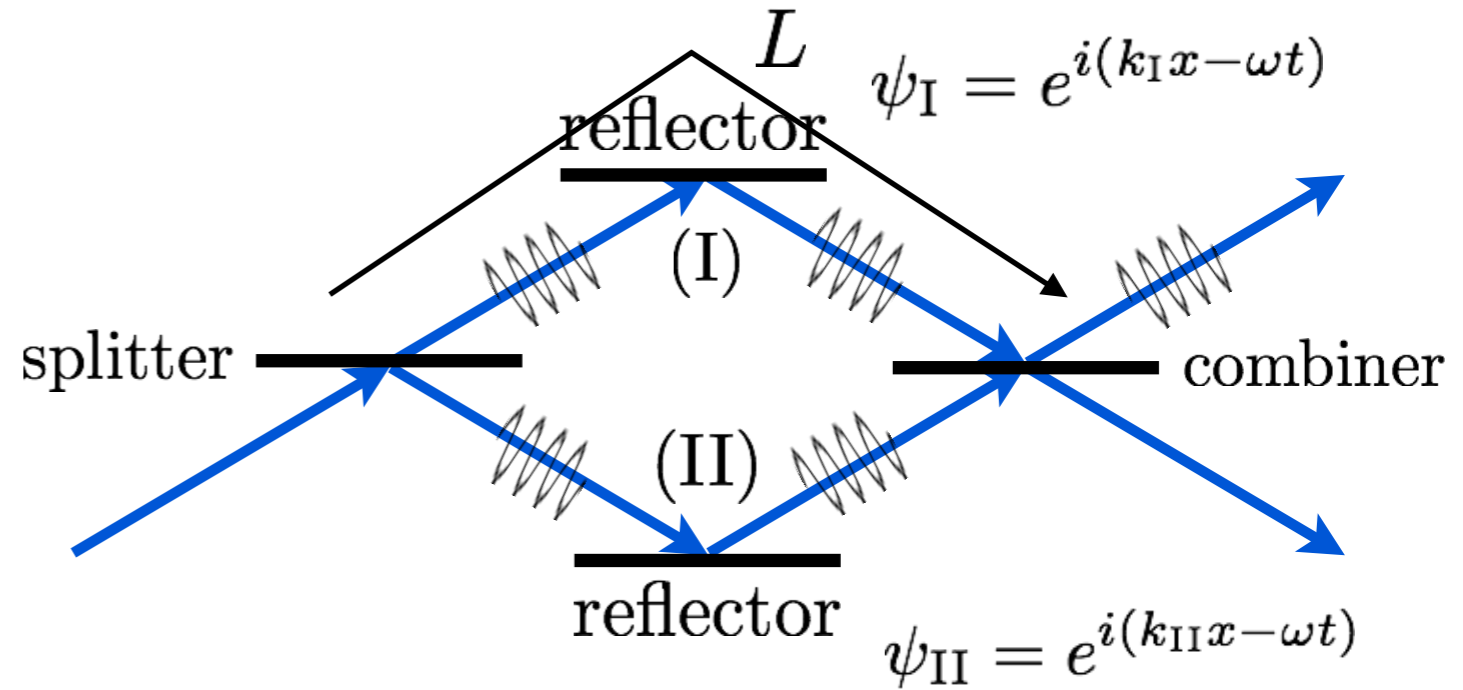
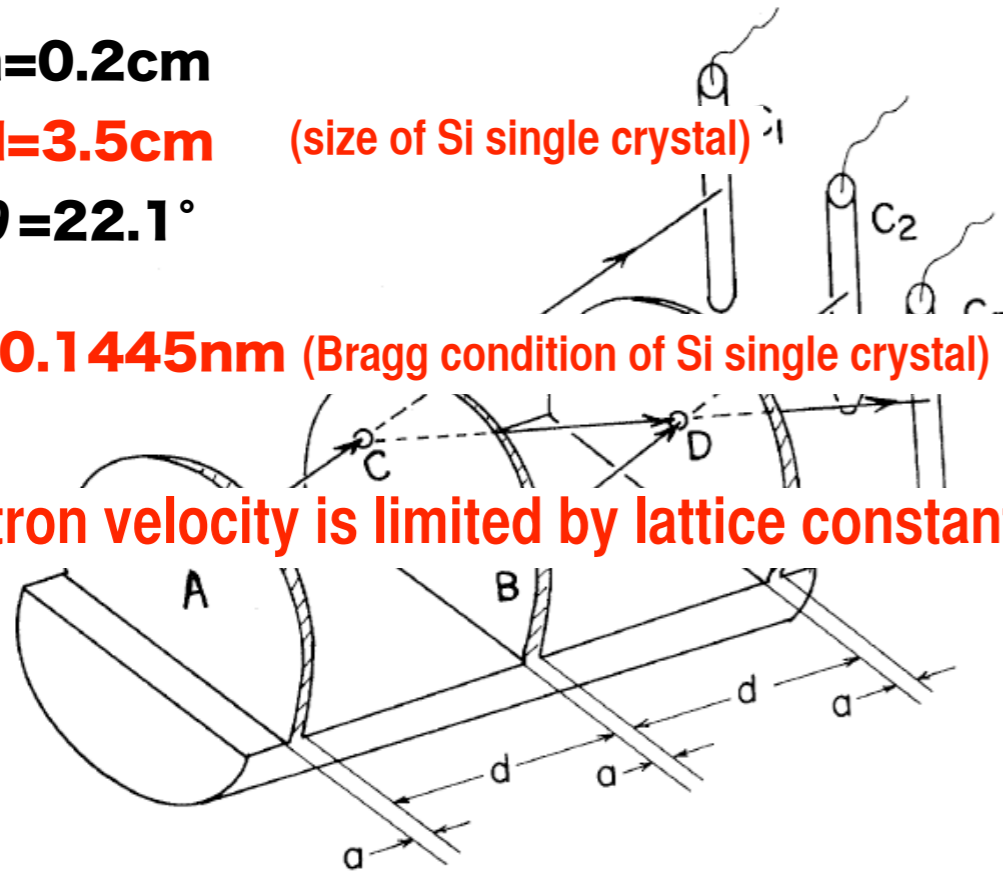
$a=0.2\text{cm}$

$d=3.5\text{cm}$  (size of Si single crystal)

$\theta=22.1^\circ$

$\lambda=0.1445\text{nm}$  (Bragg condition of Si single crystal)

neutron velocity is limited by lattice constant



$$k_I = \frac{\sqrt{2m_n(E_0 + U)}}{\hbar}$$

$$\phi_I = k_I L$$

$$k_{II} = \frac{\sqrt{2m_n(E_0 + U + \Delta U)}}{\hbar}$$

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larger interferometer

$$\Delta\phi = \phi_{II} - \phi_I \simeq \sqrt{\frac{m_n c^2 L \Delta U}{2E}} \frac{1}{\hbar c}$$

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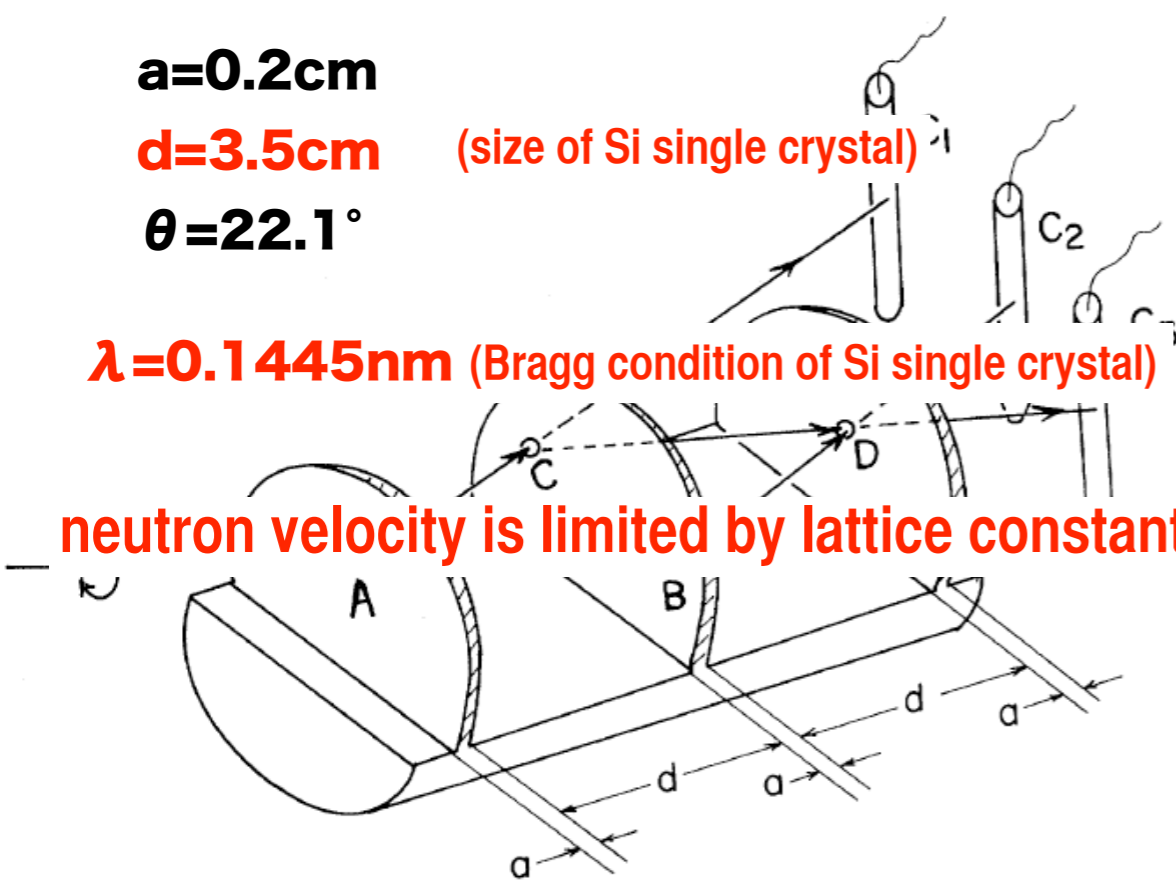
$a=0.2\text{cm}$

$d=3.5\text{cm}$  (size of Si single crystal)

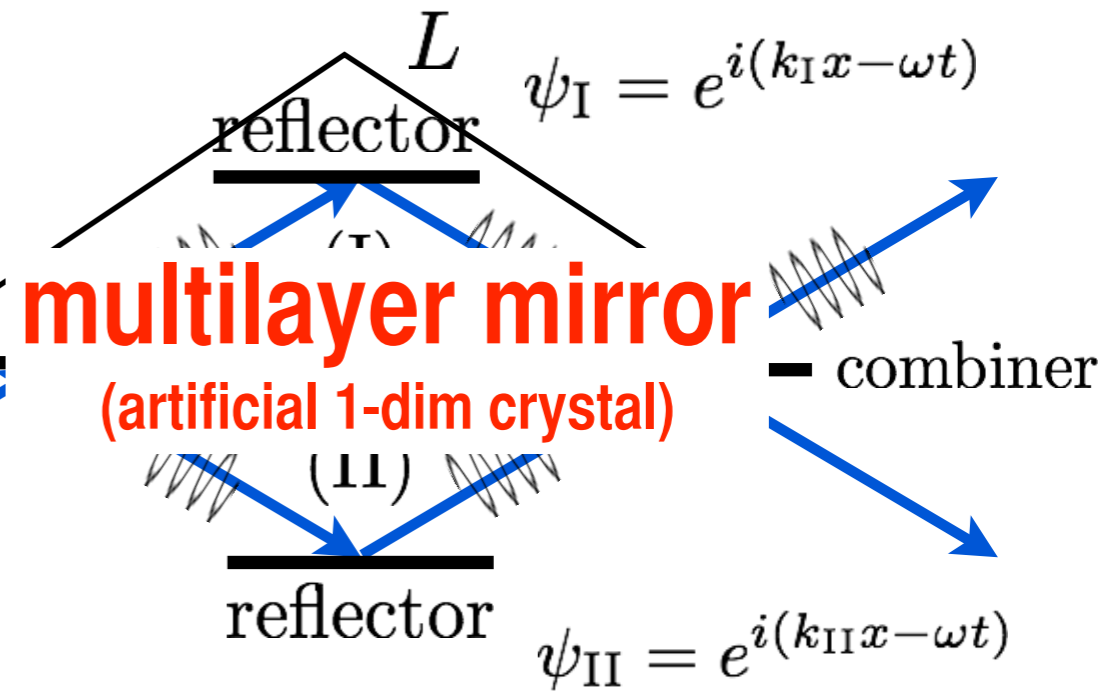
$\theta=22.1^\circ$

$\lambda=0.1445\text{nm}$  (Bragg condition of Si single crystal)

neutron velocity is limited by lattice constant



splitter



**multilayer mirror**  
(artificial 1-dim crystal)

$$k_I = \frac{\sqrt{2m_n(E_0 + U)}}{\hbar}$$

$$k_{II} = \frac{\sqrt{2m_n(E_0 + U + \Delta U)}}{\hbar}$$

$$\phi_I = k_I L$$

$$\phi_{II} = k_{II} L$$

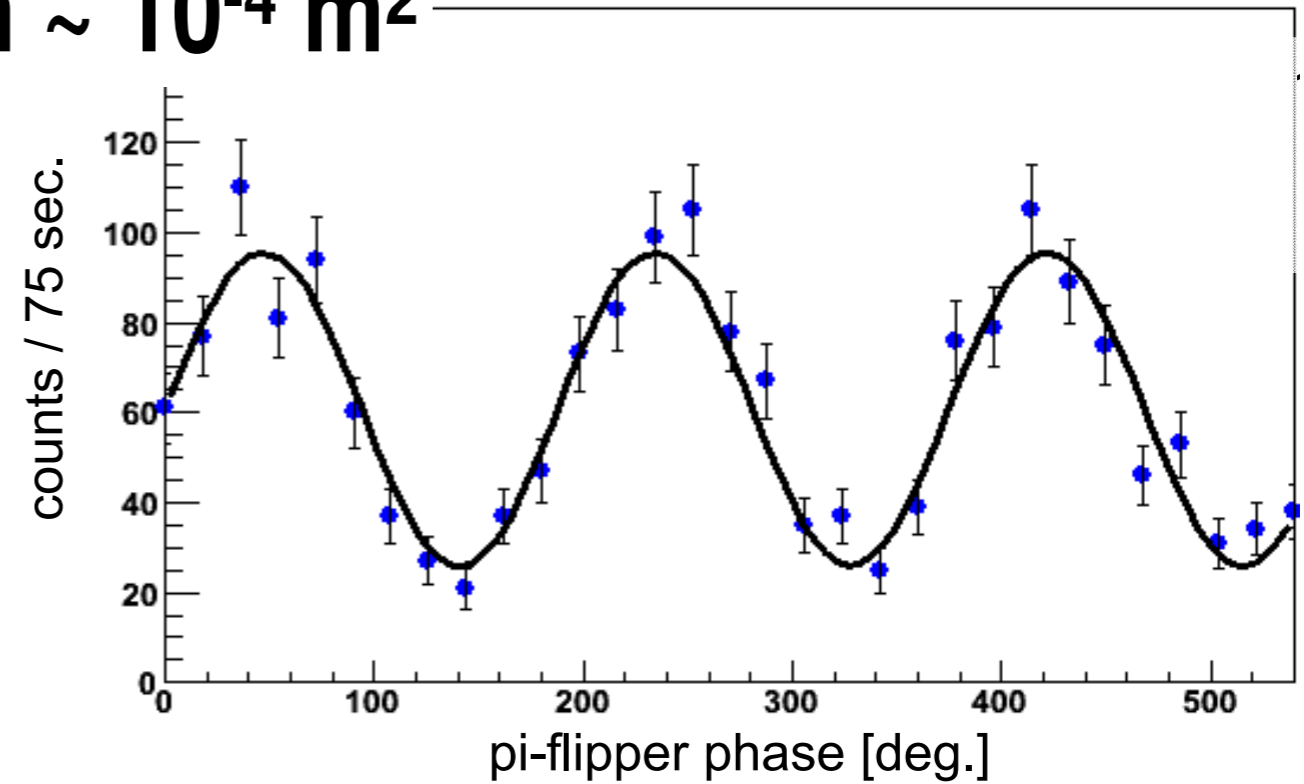
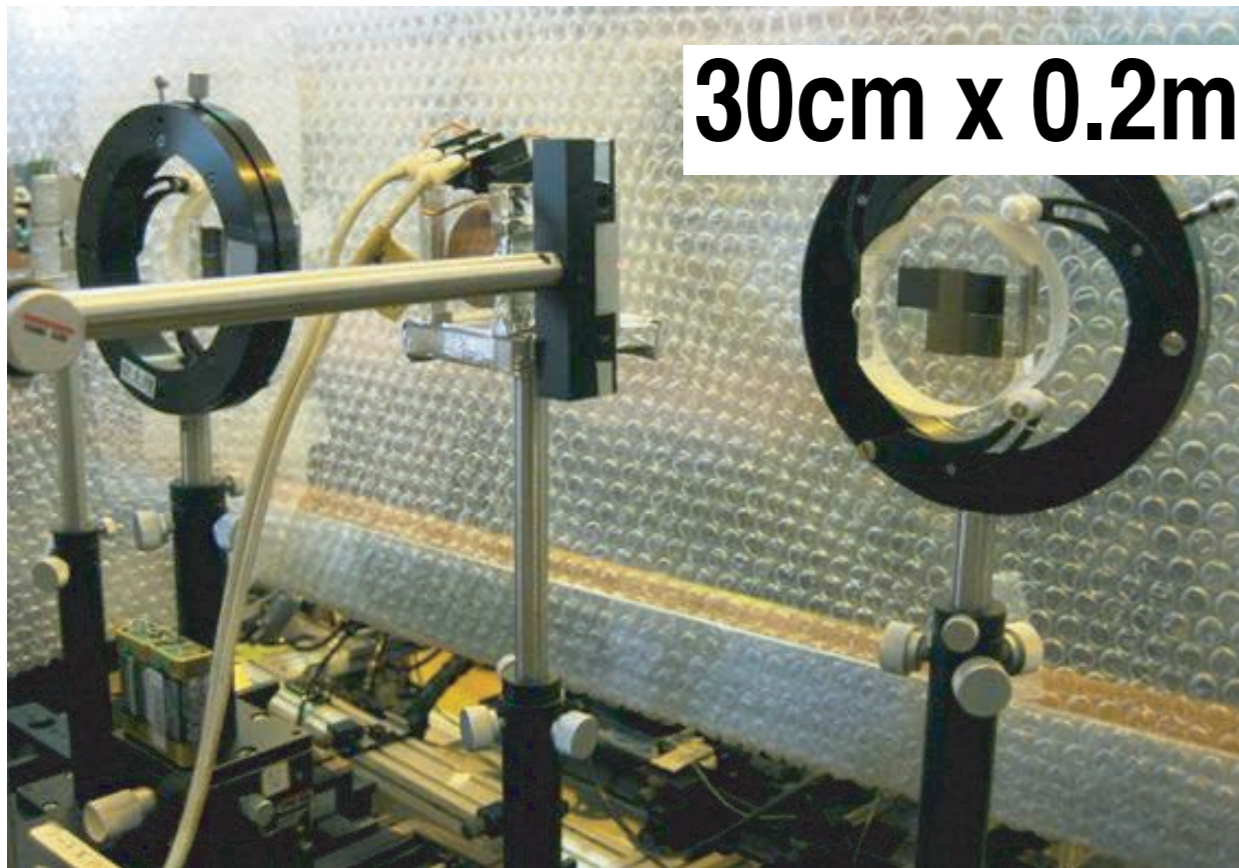
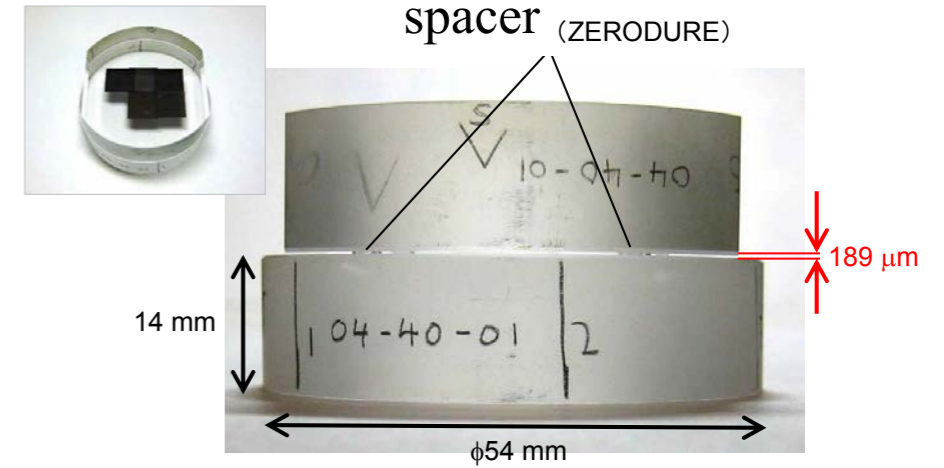
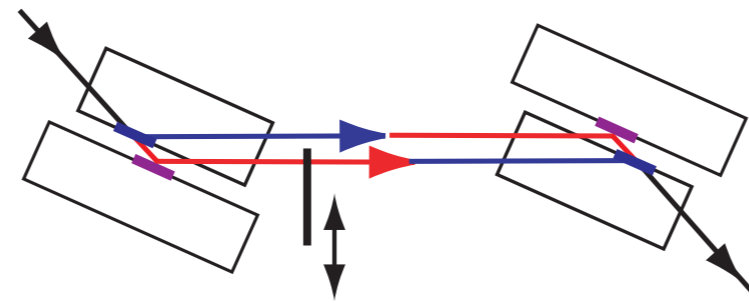
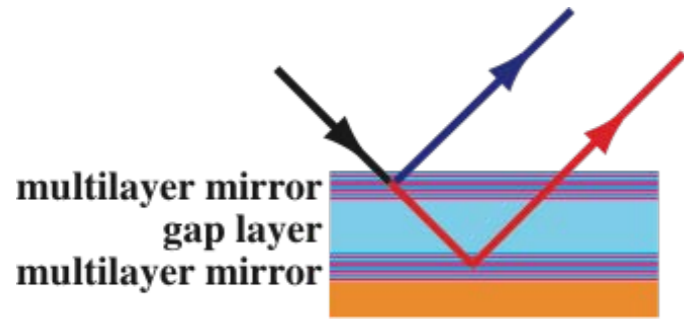
larger interferometer

$$\Delta\phi = \phi_{II} - \phi_I \simeq \sqrt{\frac{m_n c^2 L \Delta U}{2E}} \frac{1}{\hbar c}$$

better statistics

slower neutron

# Mirror Alignment





# Multilayer Neutron Interferometer

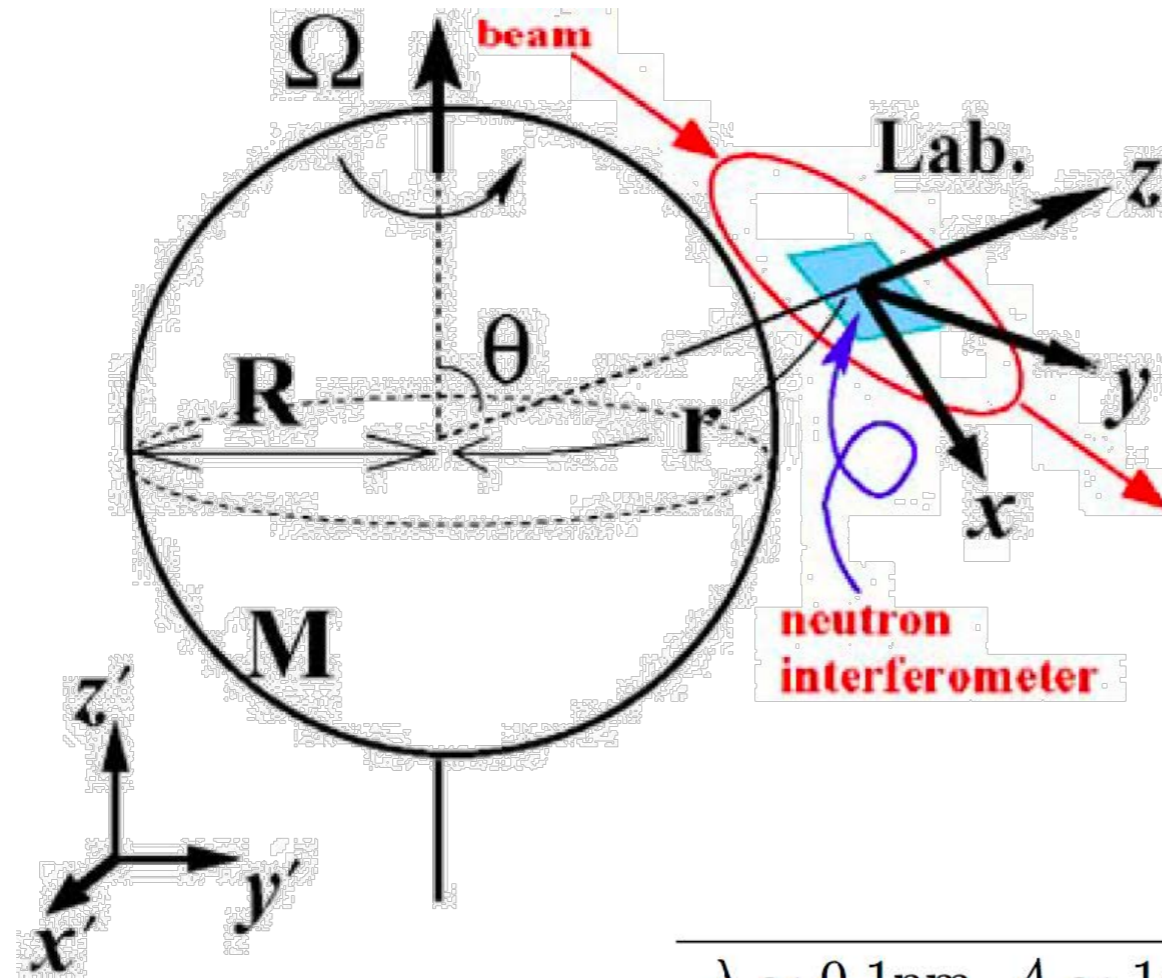


larger interferometer

$$\Delta\phi = \phi_{II} - \phi_I \simeq \sqrt{\frac{m_n c^2 L \Delta U}{2E}} \frac{1}{\hbar c}$$

better statistics

slower neutron



$$\phi = -\frac{GM}{r}$$

$$\mathbf{S} = \frac{\hbar}{2}\boldsymbol{\sigma}$$

$$\mathbf{L} = \mathbf{r} \times \mathbf{p}$$

**COW**

$$\mathcal{H} = \frac{\mathbf{p}^2}{2m} + \boxed{m\phi} - \boldsymbol{\Omega} \cdot (\mathbf{L} + \mathbf{S})$$

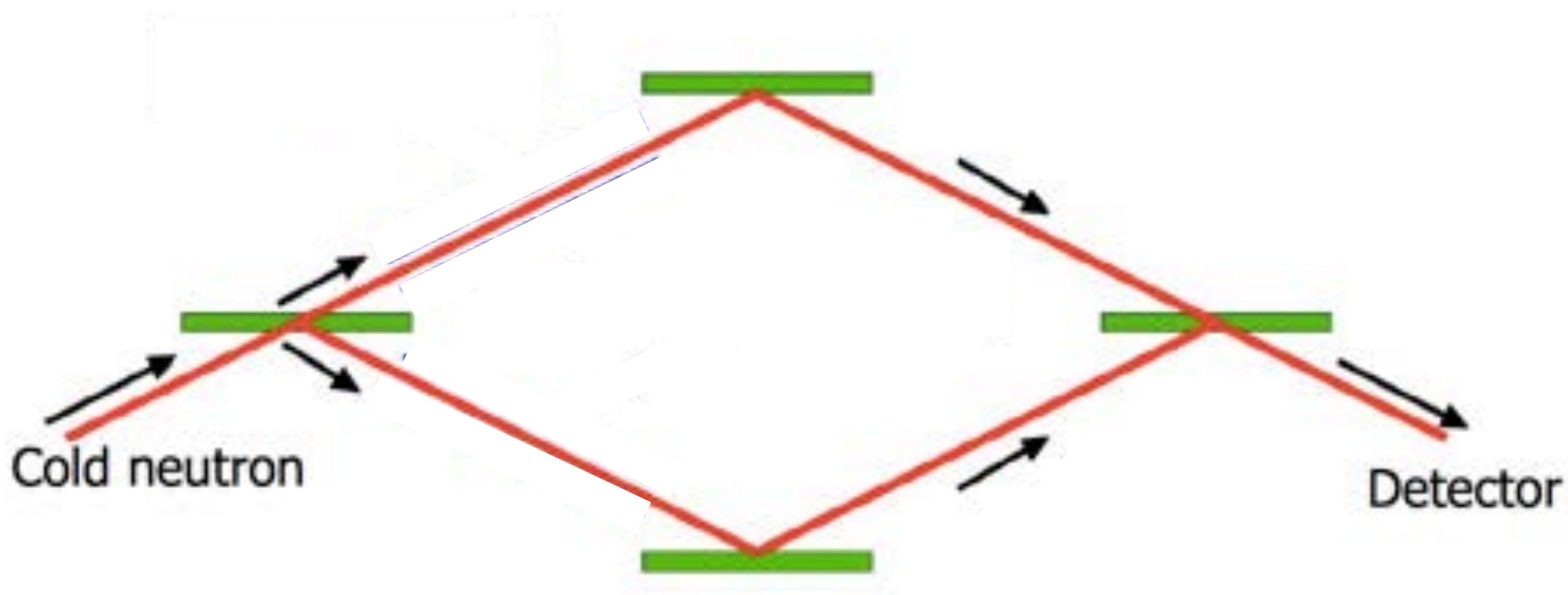
$$+ \frac{1}{c^2} \left( -\frac{\mathbf{p}^4}{8m^3} + \frac{m}{2}\phi^2 + \frac{3}{2m}\mathbf{p} \cdot (\phi\mathbf{p}) + \frac{3GM}{2mr^3}\mathbf{L} \cdot \mathbf{S} + \boxed{\frac{4GMR^2}{5r^3}\boldsymbol{\Omega} \cdot (\mathbf{L} + \mathbf{S})} + \frac{6GMR^2}{5r^5}\mathbf{S} \cdot (\mathbf{r} \times (\mathbf{r} \times \boldsymbol{\Omega})) \right)$$

$\lambda \sim 0.1\text{nm}, A \sim 1\text{cm} \times 1\text{cm}$	$m\phi$	$\frac{4GMR^2\boldsymbol{\Omega} \cdot (\mathbf{L} + \mathbf{S})}{5r^3c^2}$
$\lambda \sim 1.0\text{nm}, A \sim 1\text{m} \times 1\text{m}$	5	$10^{-10}$
	$10^5$	$\boxed{10^{-6}}$

**accessible with J-PARC**

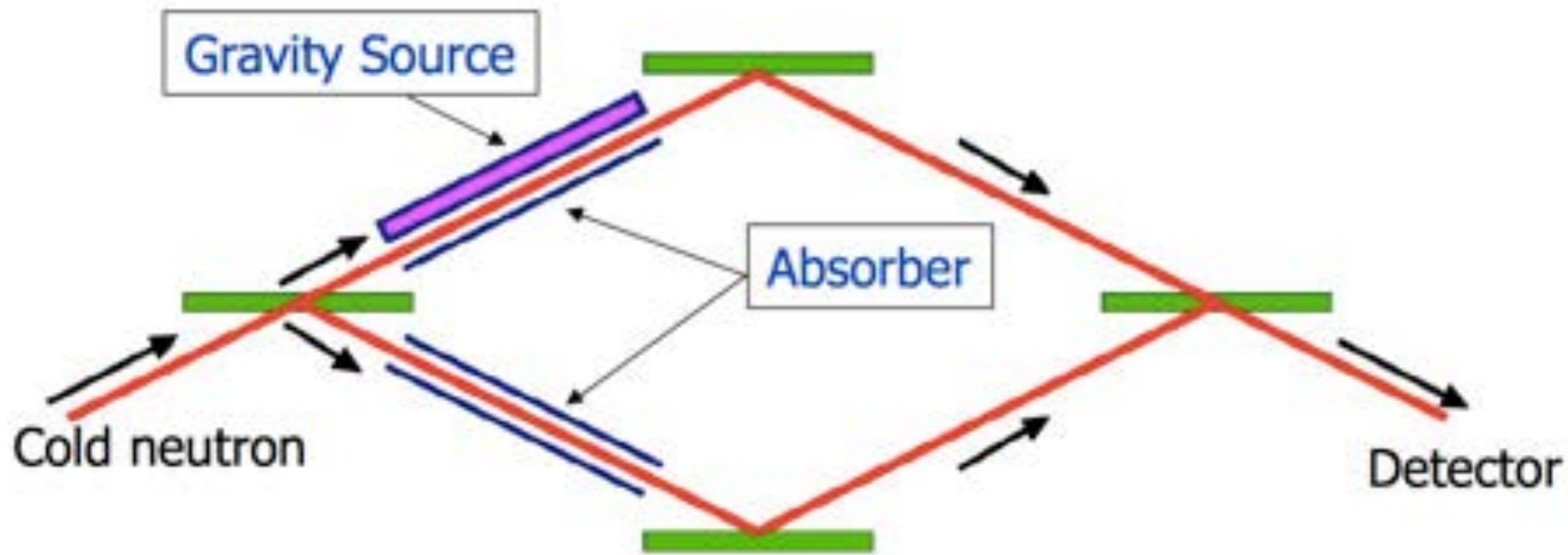
**Lense-Thirring**

# Mach-Zehnder configuration

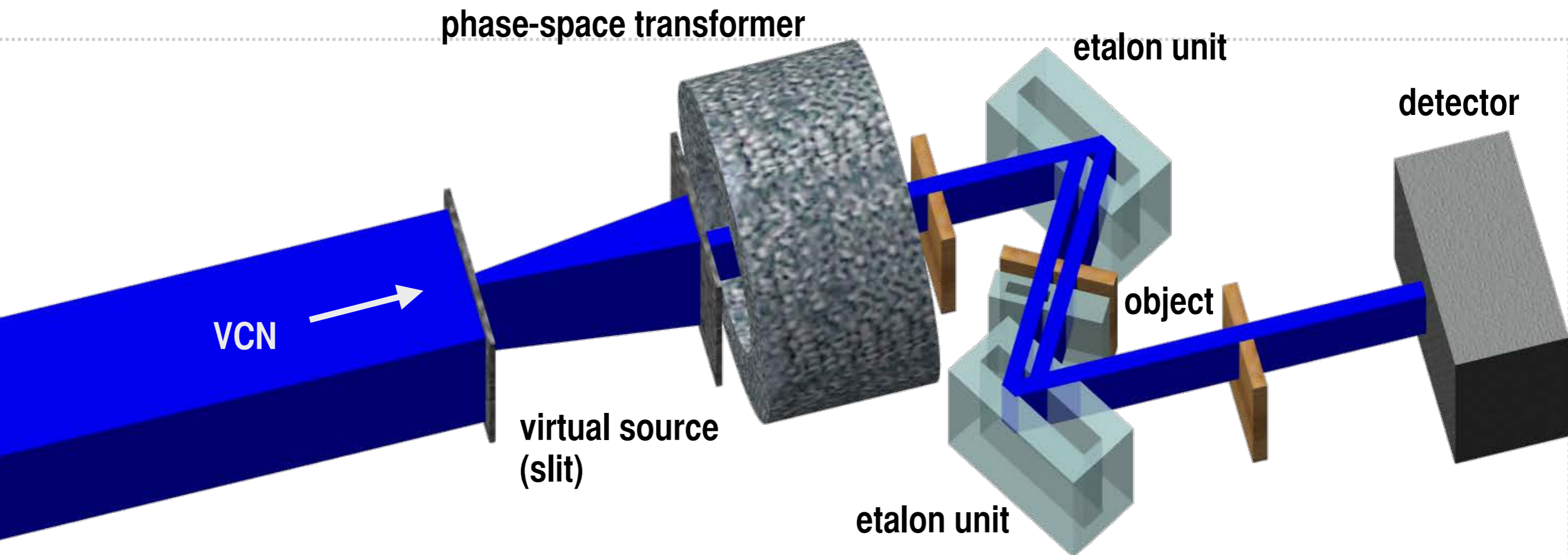




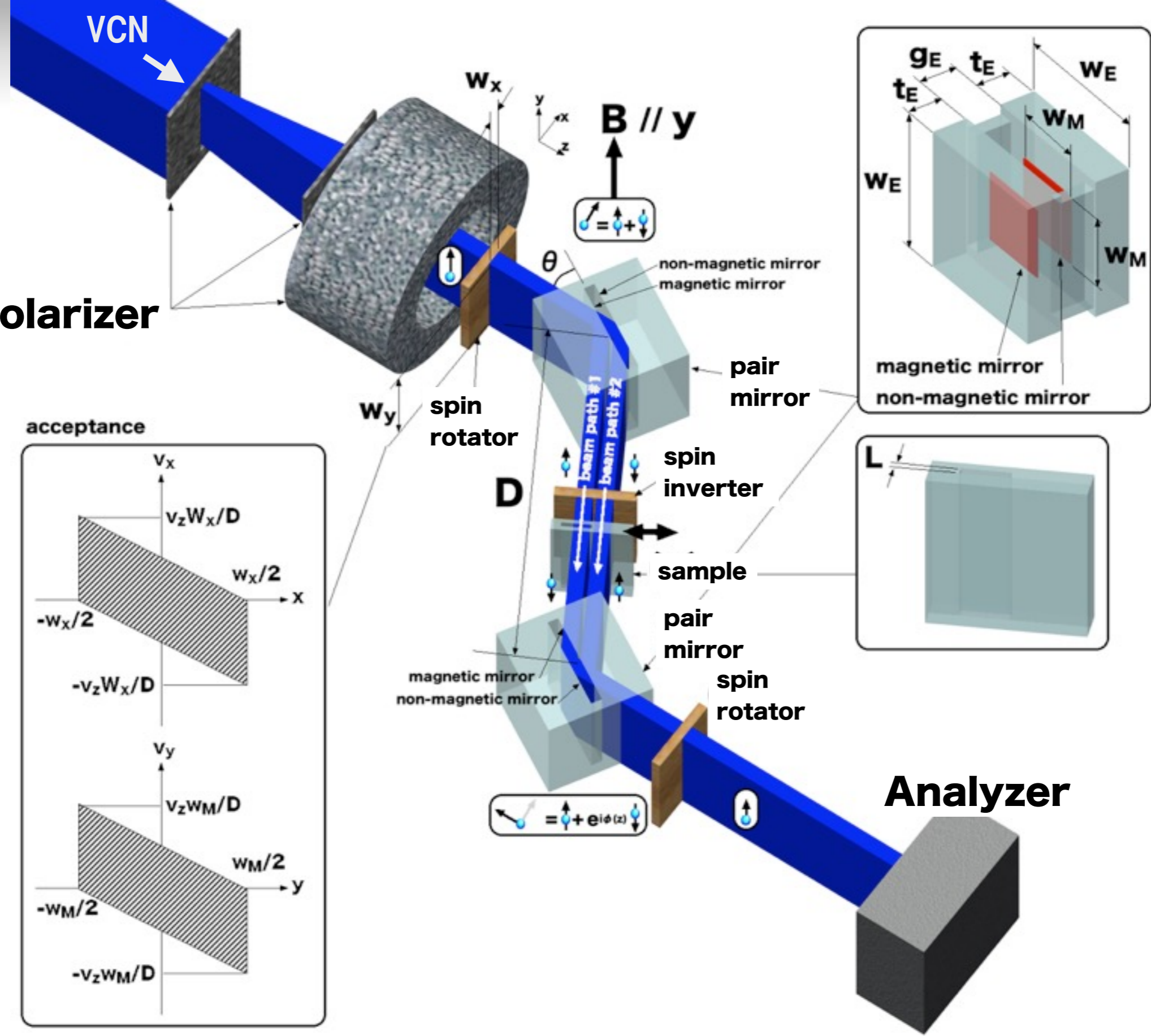
# New Interaction Search (mm-range)



# VCN Interferometry



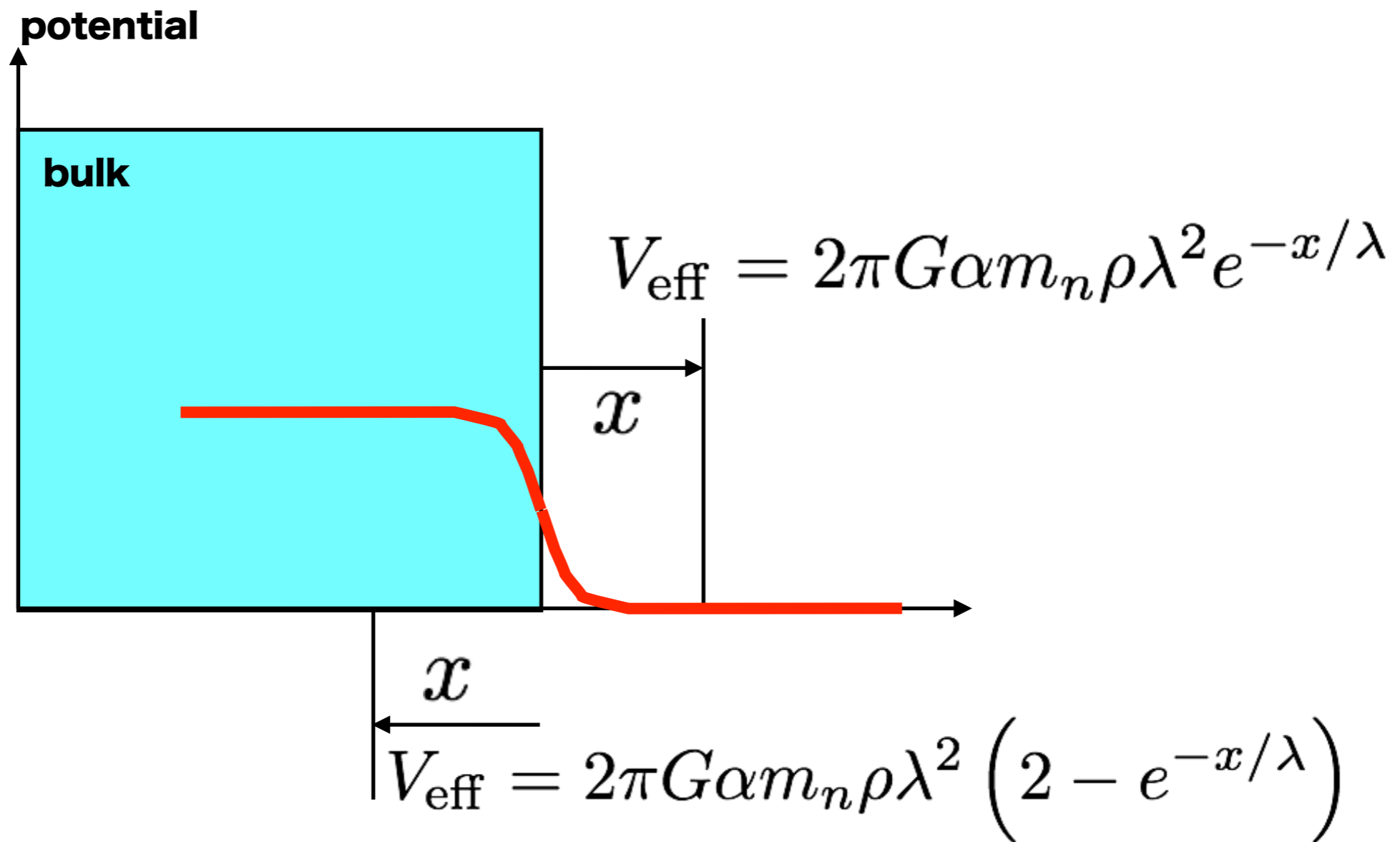
# Polarizer





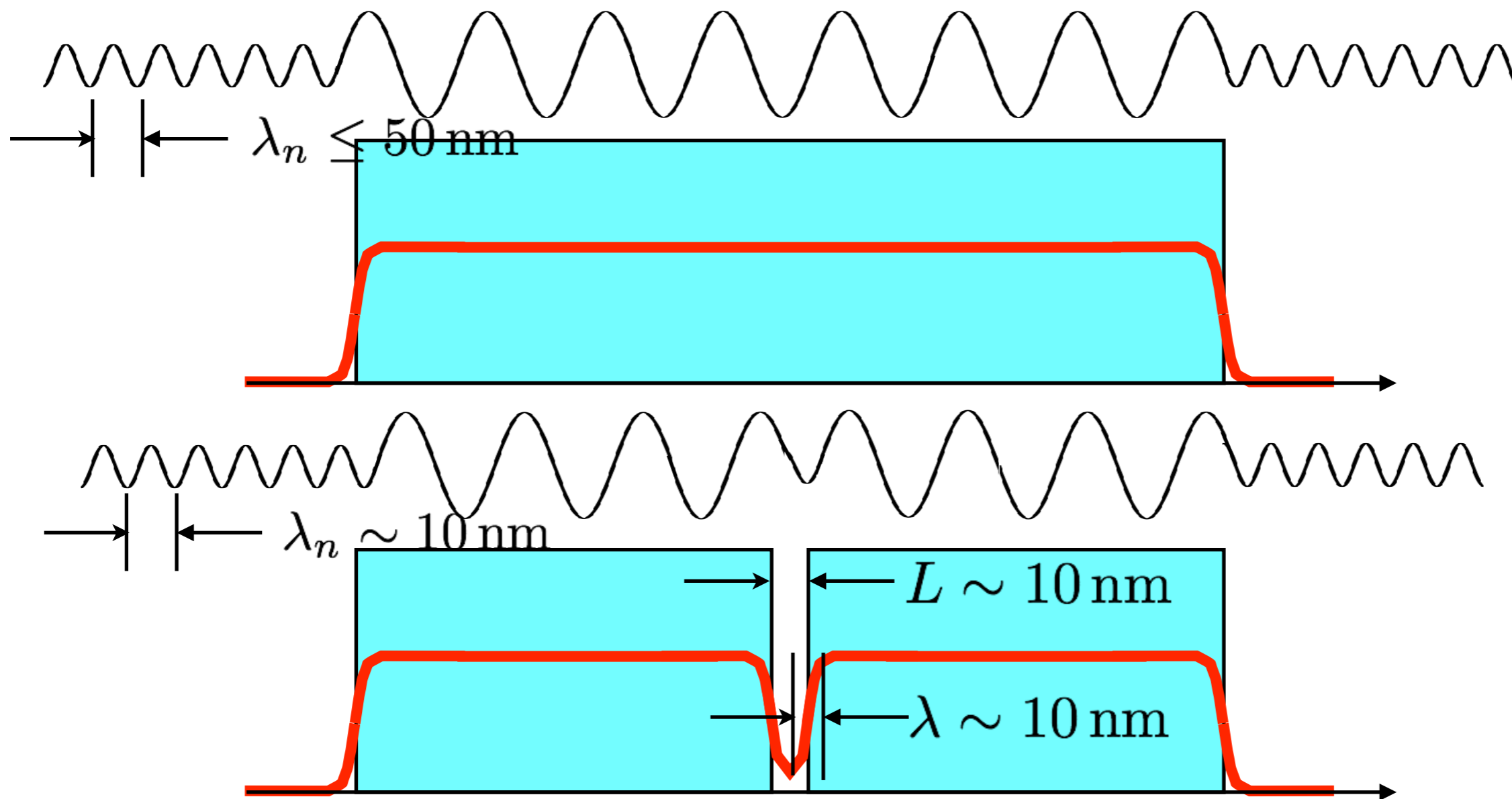
# Potential of Hypothetical Yukawa-interactions near the Bulk Surface

$$V_G(r) = -\frac{GM}{r} \alpha e^{-r/\lambda}$$



# Parametric Resonance due to the Yukawa Interactions

$$V_G(r) = -\frac{GM}{r} \alpha e^{-r/\lambda}$$



Gudkov, Shimizu, Greene, PRC 83 (2011) 025501

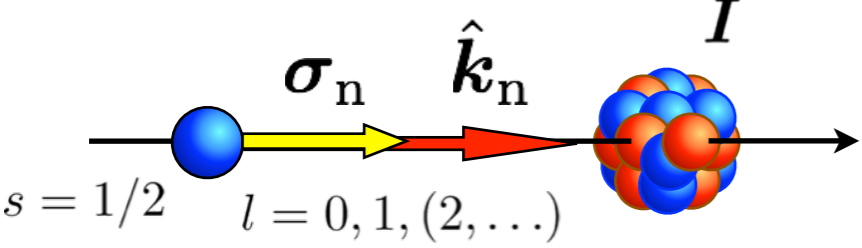
# Epithermal Neutron Optics



# Compound States

**P-violation**

$$\sigma = \sigma_0 + \Delta\sigma(\sigma_n \cdot \hat{k}_n)$$



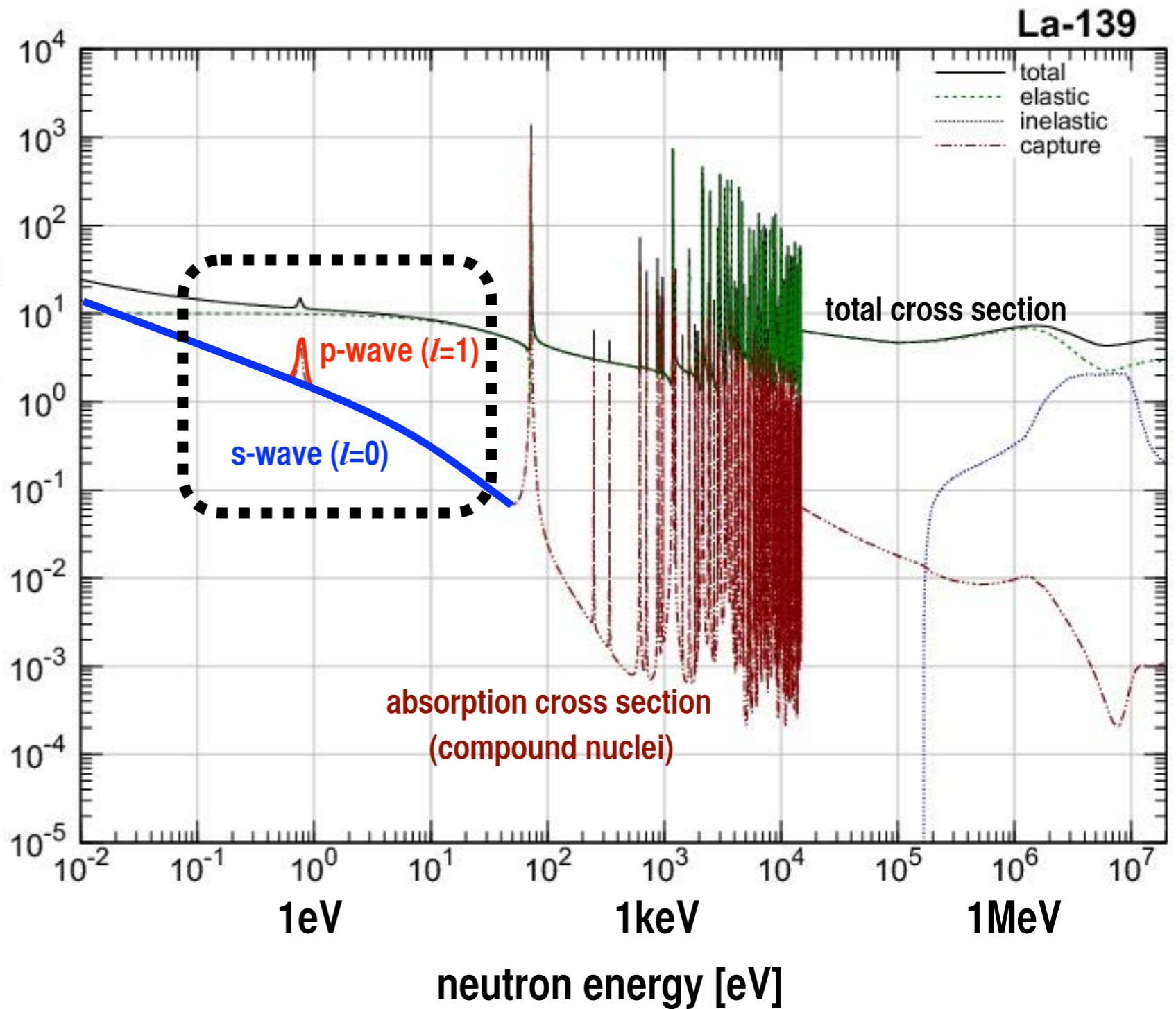
$(E_n=0.75\text{eV})$

$(E_n=-48.6\text{eV})$

5160.902 keV

$^{140}\text{La}$

cross section [b]



thermal

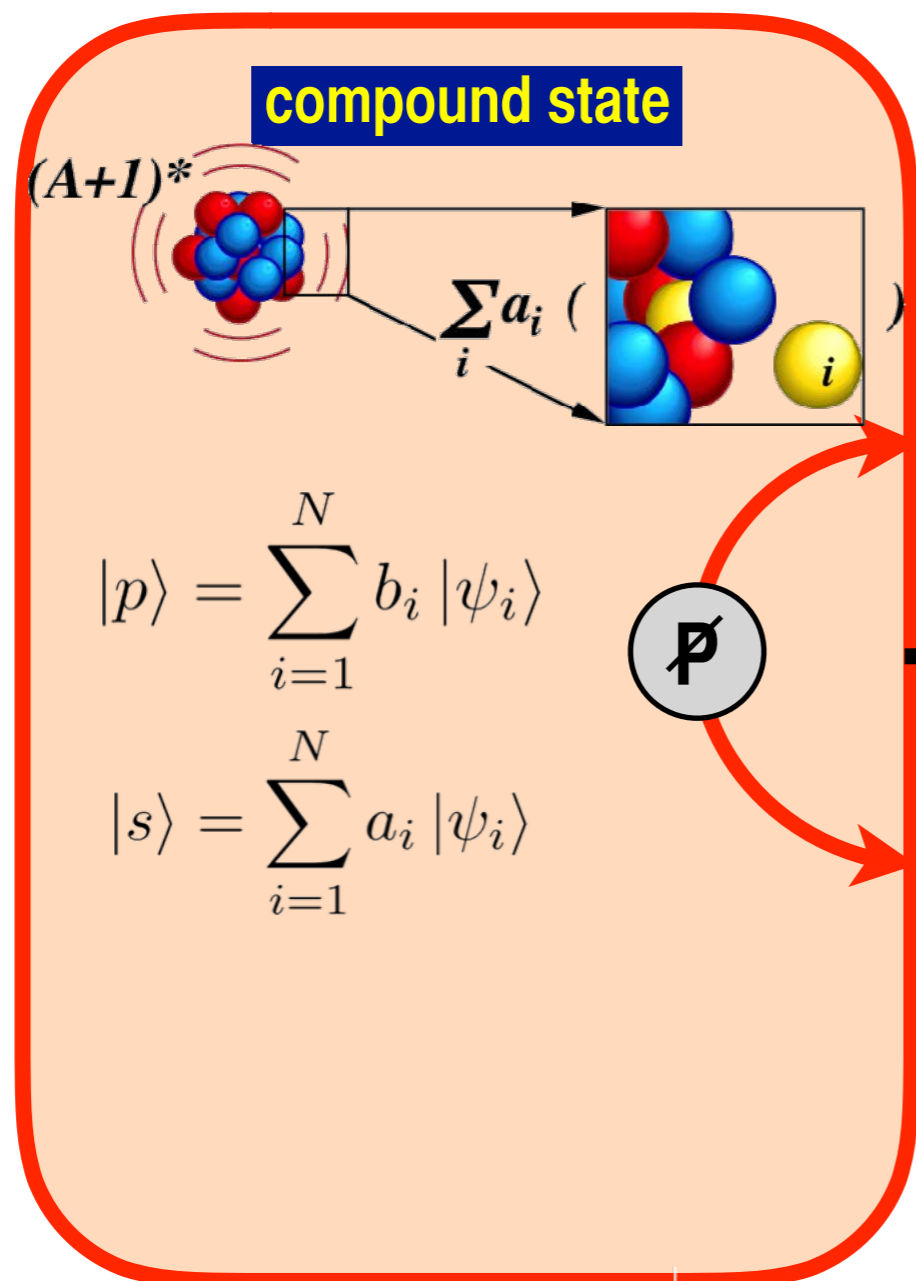
epithermal

fast

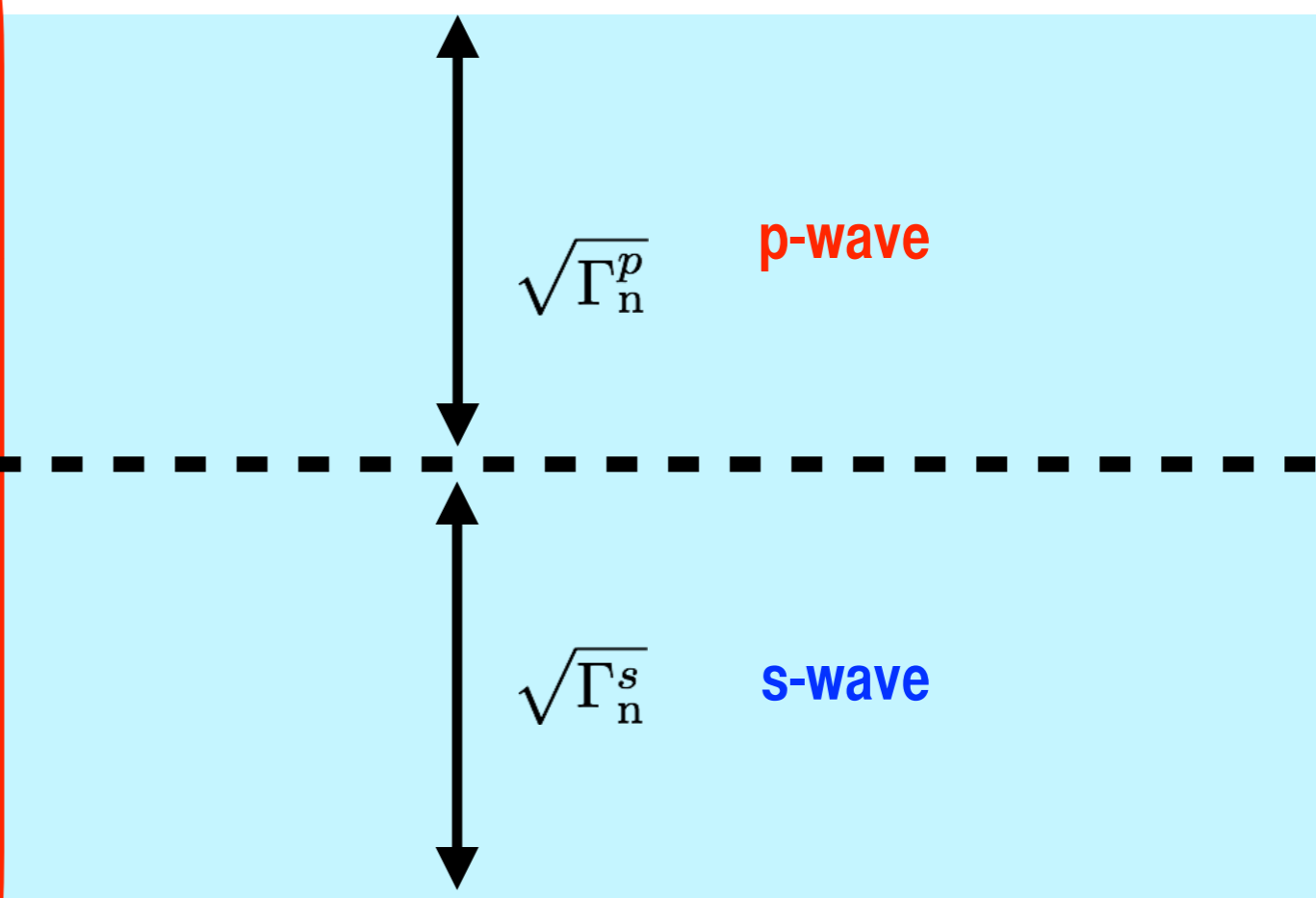
# Dynamical Enhancement



entrance channel



exit channel



~ P-violation in NN interaction

$$\langle s|W|p\rangle = \sum_{i,j} a_i^* b_j \langle \psi_i|W|\psi_j\rangle \sim \frac{1}{\sqrt{N}} \frac{1}{\sqrt{N}} \langle W \rangle \sqrt{N}$$

randomness of expansion coefficients

$$N \sim \frac{10^6 \text{ eV}}{\frac{\Delta E}{D}} \sim 10^5$$

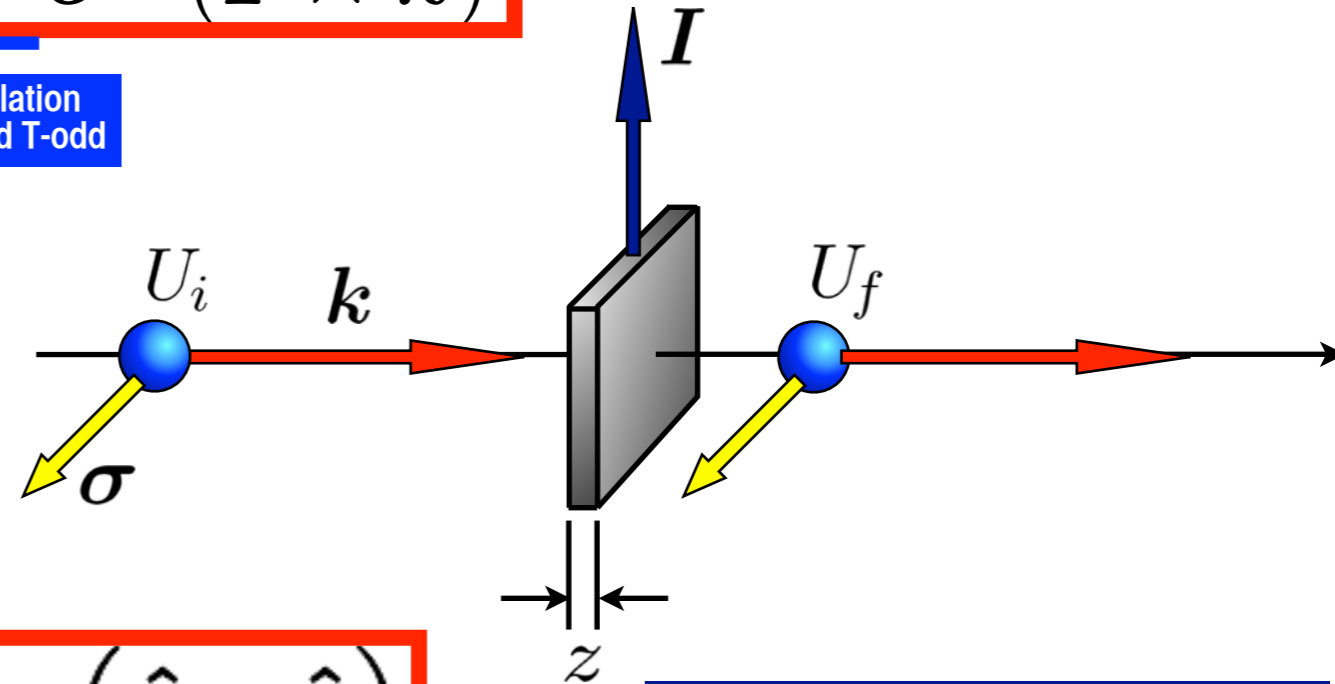
10 eV

# T-violation in Neutron Optics

$$f = \underbrace{A'}_{\substack{\text{Spin Independent} \\ \text{P-even T-even}}} + \underbrace{B'\sigma \cdot \hat{I}}_{\substack{\text{Spin Dependent} \\ \text{P-even T-even}}} + \underbrace{C'\sigma \cdot \hat{k}}_{\substack{\text{P-violation} \\ \text{P-odd T-even}}} + \underbrace{D'\sigma \cdot (\hat{I} \times \hat{k})}_{\substack{\text{T-violation} \\ \text{P-odd T-odd}}}$$

$$U_f = \delta U_i$$

$$\delta = e^{i(n-1)kz} \quad n = 1 + \frac{2\pi\rho}{k^2} f$$



$$\delta = \underbrace{A}_{\substack{\text{Spin Independent} \\ \text{P-even T-even}}} + \underbrace{B\sigma \cdot \hat{I}}_{\substack{\text{Spin Dependent} \\ \text{P-even T-even}}} + \underbrace{C\sigma \cdot \hat{k}}_{\substack{\text{P-violation} \\ \text{P-odd T-even}}} + \underbrace{D\sigma \cdot (\hat{I} \times \hat{k})}_{\substack{\text{T-violation} \\ \text{P-odd T-odd}}}$$

fake T-odd negligible

$$A = e^{iZA'} \cos b$$

$$B = ie^{iZA'} \frac{\sin b}{b} ZB'$$

$$Z = \frac{2\pi\rho}{k} z$$

$$C = ie^{iZA'} \frac{\sin b}{b} ZC'$$

$$b = Z(B'^2 + C'^2 + D'^2)^{1/2}$$

$$D = ie^{iZA'} \frac{\sin b}{b} ZD'$$

$D \neq 0 \Rightarrow D' \neq 0$

validity of this description can be checked via the consistency among A, B, C



# Present/Future Neutron Optics

## Summary

**High Phase-space Density (Brilliance)  
enables flexible optical control**

### Optics

**Precision machining techniques  
are delivering practically applicable new opportunities  
with metal substrate super mirrors.**

**Also control of neutron waves  
interferometry and spatial**

**Epithermal spin optics as a new approach to new physics  
(Refractive optics -> afternoon)**