Self-consistent, angular-momentum-dominated hadron beams for space charge mitigation

Austin Hoover Space Charge Mini-Workshop Knoxville, TN, USA October 26, 2022

ORNL is managed by UT-Battelle, LLC for the US Department of Energy



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Summary slide, 5th ICFA mini-workshop on Space Charge Theme: Bridging the gap in space charge dynamics

In 1-2 sentences, summarize the content of this presentation (If relevant, specify type of facility, species, tune shift): I review several proposed techniques to control the density and angular momentum of hadron beams for the purpose of space charge mitigation.

From your perspective, where is the gap regarding space charge effects? (understanding/control/mitigation/prediction/?) How to increase the beam intensity in low-energy hadron rings

What is needed to bridge this gap? New lattice design (nonlinear optics, strong coupling) and beam shaping techniques (painting)

Outline

- Angular-momentum-dominated (AMD) beams
- Self-consistent beams
- Beam shaping
- Questions/research directions

AMD beams have small 4D emittance — can exist in round or flat state

$$\boldsymbol{\Sigma} = \begin{bmatrix} \langle xx \rangle & \langle xx' \rangle & \langle xy \rangle & \langle xy' \rangle \\ \langle xx' \rangle & \langle x'x' \rangle & \langle yx' \rangle & \langle x'y' \rangle \\ \langle xy \rangle & \langle yx' \rangle & \langle yy \rangle & \langle yy' \rangle \\ \langle xy' \rangle & \langle x'y' \rangle & \langle yy' \rangle & \langle y'y' \rangle \end{bmatrix} = \boldsymbol{V} \begin{bmatrix} \varepsilon_1 & 0 & 0 & 0 \\ 0 & \varepsilon_1 & 0 & 0 \\ 0 & 0 & \varepsilon_2 & 0 \\ 0 & 0 & 0 & \varepsilon_2 \end{bmatrix} \boldsymbol{V}^T$$

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Circular modes for flat beams in the LHC

A. Burov Phys. Rev. ST Accel. Beams **16**, 061002 – Published 24 June 2013



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"Round Colliding Beams" As a Way to Integrability: Theory and Simulations for Tevatron

V.V. Danilov and V.D. Shiltsev

12th Int. Particle Acc. Conf. ISBN: 978-3-95450-214-1 IPAC2021, Campinas, SP, Brazil ISSN: 2673-5490 doi:10.18429/JACo

azil JACoW Publishing doi:10.18429/JACoW-IPAC2021-TUPAB002

ROUND COLLIDING BEAMS: SUCCESSFUL OPERATION EXPERIENCE

D. Shwartz^{†1}, O. Belikov, D. Berkaev, D. Burenkov, V. Denisov, A. Kasaev, A. Kirpotin, S. Kladov, I. Koop¹, A. Krasnov, A. Kupurzhanov, G. Kurkin, M. Lyalin, A. Lysenko, S. Motygin, E. Perevedentsev¹, V. Prosvetov, Yu. Rogovsky¹, A. Semenov, A. Senchenko, L. Serdakov, D. Shatilov, P. Shatunov, Yu. Shatunov¹, M. Timoshenko, I. Zemlyansky, Yu. Zharinov Budker Institute of Nuclear Physics, Novosibirsk, 630090, Russia
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AMD beams could suppress particle-core resonances



Effects of beam spinning on the fourth-order particle resonance of 3D bunched beams in high-intensity linear accelerators

Yoo-Lim Cheon, Seok-Ho Moon, Moses Chung, and Dong-O Jeon Phys. Rev. Accel. Beams **25**, 064002 – Published 10 June 2022

Outline

- Angular-momentum-dominated (AMD) beams
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Self-consistent beam = Vlasov equilibrium with linear internal space charge forces



The KV distribution is not the only solution

{n, m} distributions:

$$f(\mathbf{x}, \mathbf{x}') = g(H_b - H) \prod_{i=1}^m \delta(\mathbf{e}_i \cdot \mathbf{x} + \mathbf{e}'_i \cdot \mathbf{x}')$$

Self-consistent time dependent two dimensional and three dimensional space charge distributions with linear force

V. Danilov, S. Cousineau, S. Henderson, and J. Holmes Phys. Rev. ST Accel. Beams **6**, 094202 – Published 29 September 2003; Erratum Phys. Rev. ST Accel. Beams **11**, 019901 (2008)

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{n, 0} KV distributions



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{2, 2} distribution — a uniform density, elliptical "vortex"

$$f = \rho \delta(X' - e_{xx}X - e_{xy}Y)\delta(Y' - e_{yx}X - e_{yy}Y),$$









- Inherits all properties of AMD beams
- Beam provides strong linear coupling in AG focusing

Physically attractive due to minimized space charge tune shift/spread



Source: G. Franchetti, Space charge in circular machines, CERN Accelerator School

Lack of higher-order multipoles may reduce nonlinear particle-core interactions



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Elliptical painting: inject particles along eigenvector of ring transfer matrix



Elliptical painting: inject particles along eigenvector of ring transfer matrix



{2, 2} Danilov distribution maintained throughout injection (with space charge)

















Surprisingly, realistic SNS injection simulations preserve leading-order features



Injection of a self-consistent beam with linear space charge force into a ring

J. A. Holmes, T. Gorlov, N. J. Evans, M. Plum, and S. Cousineau Phys. Rev. Accel. Beams **21**, 124403 – Published 17 December 2018 Surprisingly, realistic SNS injection simulations preserve leading-order features





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J. A. Holmes, T. Gorlov, N. J. Evans, M. Plum, and S. Cousineau Phys. Rev. Accel. Beams **21**, 124403 – Published 17 December 2018

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Questions/research directions

- Best-case performance of elliptical painting
 - Reduction in tune shift/spread
 - Minimum $C = \sqrt{\varepsilon_1 \varepsilon_2 / \varepsilon_x \varepsilon_y}$
- Practicality
 - Proof-of-principle experiment at the SNS
 - Feasibility in collider complex
- Long-term beam stability
 - Halo formation
 - Acceleration, IBS
 - Necessity of circular mode optics
- {3, 3} distribution?
- Theoretical studies?

Extra slides

AMD beams can be produced within a solenoid at the source



FIG. 4 (color online). Vertical (blue) and horizontal (red) rms emittances at the exit of the EMTEX beam line as functions of the solenoid field strength. All other settings were kept constant. Shown are results from measurements (dots), from application of the 4d-envelope model for coupled lattices (dashed line), and from tracking simulations (dotted line). With respect to Fig. 2, the gradients of the skew quadrupole triplet are inverted.



Experimental Proof of Adjustable Single-Knob Ion Beam Emittance Partitioning

L. Groening, M. Maier, C. Xiao, L. Dahl, P. Gerhard, O. K. Kester, S. Mickat, H. Vormann, M. Vossberg, and M. Chung

Phys. Rev. Lett. 113, 264802 – Published 30 December 2014







Nonlinear fringe fields can degrade beam quality near difference resonance



Linear coupling (split tunes) alleviates this problem



Linear coupling can also be provided by the beam



Uniform density ellipsoidal *electron* distributions can be generated with properly shaped laser pulses (the pancake regime)



[Citation]

A more general KV distribution



$$f = \frac{N_b \sqrt{|\xi|}}{\pi^2} \,\delta(I_{\xi} - 1).$$

 $I_{\xi} = \mathbf{z}^T Q^T P^T \xi P Q \mathbf{z},$

Class of Generalized Kapchinskij-Vladimirskij Solutions and Associated Envelope Equations for High-Intensity Charged-Particle Beams

Hong Qin and Ronald C. Davidson Phys. Rev. Lett. **110**, 064803 – Published 5 February 2013



